# The Ether-Drift Experiment and the Determination of the Absolute Motion of the Earth 

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The Ether-Drift Experiment, Historical 1878-1881

THE general acceptance of the theory that light consists of wave motion in a luminiferous ether made it necessary to determine the essential properties of the ether which will enable it to transmit the waves of light and to account for optical phenomena in general. Theories of the ether are intimately associated with theories of the structure of matter and these are among the most fundamental in the whole domain of physical science. The ether was presumed to fill all space, even that occupied by material bodies, and yet to allow all bodies to move through it with apparent perfect freedom. The question of whether the ether is carried along by moving bodies such as the earth has been considered since the early days of the wave theory. The discovery of the aberration of light, in 1728 , was soon followed by an explanation according to the then accepted corpuscular theory of light. The effect was attributed to a simple composition of the velocity of light with the velocity of the earth in its orbit. Fresnel proposed an explanation based on the wave theory, which has been generally accepted, which presumes first that the ether is at rest in free space; and, second, that the "ether density" is different in different substances and that the velocity of propagation of light in any substance varies inversely as the square root of the ether density. These two hypotheses give a complete and satisfactory explanation of aberration; the second is considered to have been proved by the experiments of Fizeau and of Michelson and Morley on the velocity of light in moving media; the first hypothesis, that of an ether at rest in space, has always been in doubt.

The first suggestion of a method for measuring the relative motion between the earth and the ether by means of an optical experiment was made by James Clerk Maxwell in the article on "Ether," which he contributed to Vol. VIII of the 9th Edition of the Encyclopaedia Britannica, published in 1878. It is assumed that the ether as a whole is at rest, that light waves are propagated in the free ether in any direction and always with the same velocity with respect to the ether and that the earth in its motion in space passes freely through the ether without disturbing it. The
experiment is based upon the argument that the apparent velocity of light would be different according to whether the observer is carried by the earth in the line in which the light is travelling or at right angles to this line. It would thus be possible to detect a relative motion between the moving earth and the stationary ether, that is to observe an "ether drift." The orbital motion of the earth has a velocity of thirty kilometers per second, while the velocity of light is ten thousand times as great, three hundred thousand kilometers per second. If it were possible to measure the direct effect of the earth's orbital motion on the apparent velocity of light, then the velocity measured in the line of motion should differ from the velocity at right angles to this line by thirty kilometers per second, that is by one part in ten thousand. This would be a "first-order effect." Maxwell explains that, since all practicable methods require that the light shall travel from one station to another and back again to the first station, a positive effect of the earth's motion on the ray going outward would be neutralized by a negative effect on the returning ray, except that on account of the motion of the observer during the time the light is travelling the neutralization would not be quite complete, and a "second-order effect," proportional to the square of the ratio of the velocity of the earth to the velocity of light, would be observable. Maxwell concludes with the statement, "The change in the time of transmission of the light on account of a relative velocity of the aether equal to that of the earth in its orbit would be only one hundred-millionth part of the whole time of transmission, and would therefore be quite insensible."

The late Professor Albert A. Michelson accepted the challenge of Maxwell's suggestion and while attending the University of Berlin in 18801881, he devised the remarkable instrument universally known as the Michelson interferometer which was especially adapted to the ether-drift experiment. ${ }^{1,2}$ In the interferometer a

[^0]beam of light is literally split in two by a "halfsilvered mirror," and the two beams of light may be made to travel paths at right angles to each other. At the end of the desired path, each beam is reflected back upon itself and the two come together where they first separated. If the two right-angled paths are optically equal, the reunited beams of light will blend with the waves in concordance. If, however, the paths of the light in the interferometer differ either in actual length or in the optical properties of the medium through which the light passes, differences of phase will result which may be observed as "interference fringes." Observation of these lringes enables one to detect exceedingly small changes in the relative velocities of the light in the two paths of the interferometer, the measurements being made in terms of the wave-length of the light.
Michelson at once applied his interferometer to detect the relative motion of the earth and the ether as proposed by Maxwell. Alexander Graham Bell provided for the construction of the new instrument, Fig. 1, which was made by


Schmidt \& Haensch of Berlin. The half-silvered mirror was placed over the central axis, and two arms at right angles, each 120 centimeters long, carried the end mirrors. The apparatus could be set with the telescope arm pointing in different ximuths and it should be possible to detect the effect of the orbital motion of the earth when the light travels in the direction of this motion and at right angles to it.
The first trials of the ether-drift experiment
vere made at the Physikalisches Institut of the

[^1]University in Berlin; but the disturbances produced by street traffic made it impossible to see the fringes except in the middle of the night. The experiment was transferred to the Observatory in Potsdam, the interferometer being mounted in a hollow place in the lower part of the brick pier which supported the big telescope. The report of the experiment, published in $1881^{3}$ (with a correction explained in the paper of 1887), ${ }^{4}$ states that, considering only the motion of the earth in its orbit, the displacement of the interference fringes to be expected would be 0.04 of the fringe width; the displacements actually observed varied from 0.004 to 0.015 of a fringe width and were considered to be merely errors of experiment. The conclusion was that the hypothesis of a stationary ether was not confirmed.

## The Michelson-Morley Experiments, Cleveland, 1887

While he was still in Europe, in 1881, Michelson was appointed to the Professorship of Physics in the newly organized Case School of Applied Science in Cleveland and thus became acquainted with the late Professor Edward W. Morley, Professor of Chemistry in Western Reserve University, these two institutions being located side by side. Professor Morley proposed several important developments in the interferometer and in the method of using it, so that it became adequate to measure the then expected effect in the ether-drift experiment. Having secured an appropriation from the Bache Fund of the National Academy of Sciences, a new interferometer was constructed, embodying these improvements; the optical parts were made by the late John A. Brashear of Pittsburgh. In order to avoid disturbances of vibration and distortion, the optical parts were mounted on a solid block of sandstone, Fig. 2, which was floated on mercury contained in a circular tank of cast iron. This support by floatation made it possible to turn the interferometer to different azimuths while observations were in progress. The practicable limit for the size of the stone base was 150

[^2]

FIG. 2. The Michelson-Morley interferometer of 1887.
centimeters square and 30 centimeters thick. In order to obtain the necessary sensitivity, the effective light path was increased by reflecting the light back and forth so that it traversed the diagonal of the square stone block eight times, giving the effect of an interferometer with an arm about 1100 centimeters in length. The expected displacement of the fringes due to a velocity equal to that of the earth in its orbit was 0.4 of a fringe width.

Michelson and Morley performed the historic experiment in the northwest room of the basement of the Main Building of Adelbert College in Cleveland in 1887; their entire series of observations was of six hours' duration, one hour at noon on each day of July 8,9 and 11 , and one hour in the evening of July 8, 9 and 12 and consisted of thirty-six "turns" of the interferometer, readings being made at each of sixteen equidistant points in each turn. The method of observation was arranged to detect the preconceived effect of the motion of the earth toward a known point in space with a given velocity, and hence no general series of observations was made. The brief series of observations was sufficient to show clearly that the effect did not have the anticipated magnitude. However, and this fact must be emphasized, the indicated effect was not zero; the sensitivity of the apparatus was such that the conclusion, published ${ }^{4}$ in 1887, stated that the observed relative motion of the earth and ether did not exceed onefourth of the earth's orbital velocity. This is quite different from a null effect now so frequently imputed to this experiment by writers on Relativity. It also seems necessary to call
attention to another historical fact: Michelsal and Morley made only the one series of obsery tions, in July, 1887, and never repeated tie ether-drift experiment at any other time, no withstanding many printed statements to 4 contrary.

In the original account of their experiment Michelson and Morley give the actual readinp for the position of the interference fringes in tie six sets of observations. The upper one of tis two long curves in Fig. 3, shows the averay


FIG. 3. Fringe displacements of the original Michelsor Morley experiments of 1887.
of the three sets of readings taken at noon, ari the lower long curve is the average for the thra sets taken in the evening. These curves show tie fringe displacements for a full turn of the interferometer, while the ether-drift effect bein sought is periodic in each half turn. To find the latter effect, the second half of the long curvei superimposed on the first half by addition, whid
ancels the full-period effect and all odd harmonics, giving the shorter curve which is the lesired half-period effect (together with any igher even harmonics which may be present). nspection shows clearly that these curves are lot of zero value, nor are the observed points cattered at random; there is a positive, systemtic effect. These full-period curves have been nalyzed by the mechanical harmonic analyzer, thich determines the true value of the halferiod effect; this, being converted into its orresponding value for the velocity of relative potion of the earth and ether, gives a velocity of 8 kilometers per second for the noon obserations, and 8.0 kilometers per second for the rening observations. In Fig. 4, the smooth


IG. 4. Velocity of ether drift observed by Michelson 1 Morley in 1887, and by Morley and Miller in 1902, 4 and 1905, compared with the velocity obtained by iller in 1925 .
urve shows the value of the ether-drift through$t$ the day for the latitude of Cleveland, as termined by the specifications of the drift bich are derived later in this report from the servations made at Mount Wilson. The two cles on this chart show the magnitude of drift tually obtained by Michelson and Morley for e noon and evening observations, indicating a
whlt wholly consistent with the later work here ported.
The fact that the result obtained by Michelson
d Morley was not negligibly small was very y set forth by Professor Hicks of University lege, Sheffield, in 1902, in his important foretical examination of the original experitt..$^{2}$ Hicks also called attention to the presence a full-period, first-order effect, which has er been sufficiently investigated; this firsteffect will be considered later.

## The Lorentz-FitzGerald Hypothesis

The Michelson-Morley experiment, which indicated that the theory of the ether was either incomplete or incorrect, attracted world-wide attention because of its fundamental character and because the result was wholly unexpected. Professor FitzGerald of Dublin, in 1891, offered an explanation for the small effect on the hypothesis that the forces binding the molecules of a solid might be modified by the motion of the solid through the ether in such a way that the dimension of the stone base of the interferometer would be shortened in the direction of motion and that this contraction might be such as to neutralize the optical effect sought in the Michelson-Morley experiment. FitzGerald did not publish this theory in a scientific journal but he expounded it in his lectures. This hypothesis was given publicity by Sir Oliver Lodge in his address on Aberration Problems and New Ether Experiments, presented to the Royal Society on March 31, 1892, which address was published in the Philosophical Transactions for the year 1893. ${ }^{5}$ Lodge has given further details of this historical fact in his recently issued autobiography. ${ }^{6}$ In 1895 Professor Lorentz of Leyden developed the theory in a systematic manner, on the supposition that the particles of all solids are held together by electrical forces; and that a motion of the body as a whole would superpose upon the electrostatic forces between the atoms a magnetic effect due to the motion. There would result a contraction of the body in the direction of motion which is proportional to the square of the ratio of the velocities of translation and of light and which would have a magnitude such as to annul the effect of ether-drift in the MichelsonMorley interferometer. ${ }^{7}$ If the contraction depends upon the physical properties of the solid, it was suggested by others that while the expected effect might be annulled in one apparatus, it might in an apparatus of different material give place to an effect other than zero, perhaps with a contrary sign.

[^3]
## The Morley-Miller Experiments, Cleveland, 1902-1906

## The interferometer of wood, 1902

At the International Congress of Physics held in Paris in connection with the International Exposition of 1900, Lord Kelvin gave an address in which he expounded certain theories of the ether, and he explained the significance of the results of the Michelson-Morley experiments as related to these theories. ${ }^{8}$ Professor Morley and the writer were present and in a later conversation with Lord Kelvin he strongly urged the repetition of the ether-drift experiment with a more powerful apparatus. Morley and Miller then constructed an interferometer designed especially to test the Lorentz-FitzGerald hypothesis. The base of this instrument was in the form of a cross, made of planks of white pine wood about 430 centimeters long, providing a light-path more than three times as long as that used by Michelson and Morley in 1887. The general dimensions, optical parts and methods of observing with this apparatus were the same as for the steel interferometer described in detail in following sections of this paper. The instrument was mounted in the northwest corner room of the basement of the Main Building of Case School of Applied Science and three series of observations were made in August, 1902, and in June, 1903, consisting of 505 turns of the interferometer. A small positive effect was observed, indicated by the square in Fig. 4, which, while slightly larger than that of the previous experiment, was still so small as to indicate that if the reduction of the observed velocity is to be attributed to the hypothetical contraction, the pine is affected by about the same amount as is the sandstone. The changes in the wooden support due to variations in humidity and temperature made it difficult to obtain accurate observations and it was decided to abandon the pine apparatus and to construct one having a base of metal for supporting the heavy parts, while the length of the optical path could be determined by various substances, wood or metal, as desired.

While planning a new apparatus, experiments were made to show that differences of magnetic

[^4]attraction on the iron parts of the instrument could not influence the observations. Massive bars of iron were suspended at the opposite ends of one of the long arms of the cross, so that one bar should be parallel to the earth's magnetic field while the other was transverse to this field, these relations being reversed on reversing the azimuth of the apparatus. Observations with this load gave the same results as before. In a further experiment, an analytical balance was placed on. one arm with which to weigh a bar of iron having a mass of about 1200 grams. It was so oriented that at one azimuth of the apparatus the bar was parallel to the lines of the earth's magnetic field, while at another it was transverse to the field. $A$ difference of half a milligram could have been detected but no such difference existed. By observing the effect produced by a known weight on one arm of the interferometer, it was shown that the earth's magnetism could not bea disturbing factor.

## Description of the new steel interferometer

An appropriation from the Rumford Fund of the American Academy of Arts and Sciences made possible the construction, in 1904, of an entirely new apparatus of steel. The design for the base of the interferometer, made by Professor F. H. Neff of the Department of Civil Engi. neering of Case School of Applied Science, provided that all optical parts and accessories should be carried by two girders of structural steel, Figs. 5, 10 and 14, each about 430 centimeters long, which intersect in the form of a cross. The purpose of this design was to secure structural symmetry and the utmost rigidity.

The steel cross rests on a circular float of wood, Fig. 5, 150 centimeters in diameter; on the under


Fig. 5. Cross section of the mercury float for the inter ferometer.
ide of the circle is an annulus of wood having an outside diameter of 150 centimeters, an inside diameter of 80 centimeters, and a thickness of 20 antimeters. This float of wood rests on mercury mitained in an annular trough of cast iron, of wich dimensions as to leave a clearance of about one centimeter around the wood, which space is flled with mercury. It requires about 275 bilograms of mercury to float the entire appaatus which weighs about 1200 kilograms. The foat is kept central by a loose-fitting centering in which sustains no pressure. The annular iron ank is supported by piers of brick or concrete at such a height as to bring the eyepiece of the observing telescope level with the eye of the observer when he takes the posture for easy ralking around with the interferometer as it otates slowly on the mercury. The cast iron trough for the mercury together with the circular rooden float are the same parts as were used in the original Michelson-Morley interferometer of 1887 and these two pieces have been continued in use by the writer to the present time. The other parts of the apparatus of 1887 have been dispersed, excepting only three of the cast iron supports for the mirrors.
The optical flat surfaces were all made in 1902 by that artist-optician, O. L. Petitdidier of Chicago, and proved to be exceptionally perfect; these consist of two plane-parallel plates, each $10.5 \times 17.5$ centimeters in size, and sixteen plane mirrors of circular shape, 10.25 centimeters in diameter. The general plan of the interferometer is shown in the diagram, Fig. 6, which, however, is not drawn to the exact scale. On a central plate, at the intersection of the arms of the cross, are mounted the half-silvered diagonal mirror, $D$, and its compensating plate, $C$, both having been aut from a single plane-parallel disk. At the outer end of each cross-arm, four of the circular mirrors are mounted in a metal plate which is supported in a vertical position. Each of the eighteen mirrors is held by springs against the points of three adjusting screws to permit the necessary adjustments for securing interference. In order to have everything about the two arms assymmetrical as possible, there is no micrometer srew for moving the end mirror parallel to itself, all the adjustment being obtained by means of the three simple screws, as for the other


Fig. 6. Plan of the optical paths in the interferometer.
mirrors. Light from the source, $S$, is rendered parallel by the triple-lens condensing system, $L$, of 15 centimeters diameter, and reaches the halfsilvered mirror, $D$. Part of this light is transmitted to the mirror, $\mathrm{I}-1$; it is successively reflected to mirrors, $2,3,4,5,6,7$, and 8 , having travelled a distance equal to about seven and a half times the length of the arm of the cross. From mirror 8 the light returns by the same path back to $D$, where it is partially reflected to the observing telescope, $T$. A second portion of the light incident on $D$ is reflected along the other arm of the cross to II-1, is reflected to and fro and is returned to $D$ and is in part transmitted to the observing telescope. In the actual apparatus, Fig. 10, the mirrors 5 and 7 are above mirrors 3 and 1 instead of at the side of them, and mirrors 6 and 8 are above mirrors 4 and 2. By this system of mirrors the effective length of the arm of the interferometer is greatly increased and in the actual apparatus it is 3203 centimeters, giving a total light-path, going and returning, of 6406 centimeters, equal to about $112,000,000$ wave-lengths of the acetylene light used in the experiment. The telescope had an aperture of 3.3 centimeters, a focal length of 35 centimeters, and a magnifying power of thirty-five diameters. The telescope is focussed on the surface of mirror 8
where, when the adjustments are completed, the interference fringes appear to be located.

The apparatus as described, consisting of the optical plane surfaces, the steel cross and the mercury tank and float, has been used by the writer in all experiments from 1904 to the present time, except that for the experiments of December, 1921, the steel cross was replaced with a base of concrete. In 1923, the small reading telescope was replaced by an astronomical telescope of 13 centimeters aperture, having a magnifying power of fifty diameters. The whole path of the light in the apparatus is enclosed; this cover was made of pine wood throughout for the experiments of 1904 ; in 1905 the cover had glass sides for all arms, thus making the apparatus wholly transparent in the horizontal plane; this arrangement, shown in Figs. 13 and 16, has been used to the present time.

## Adjustment of the interferometer

When the mirrors are in position, the distances between them, about 425 centimeters, are compared by means of light wooden rods and the mirrors are adjusted so that the two light-paths, each consisting of eight different portions, are approximately equal. Sodium light from the common laboratory type of sodium lamp is used to establish interference; by observing the visibility maxima of the sodium interference system, the adjustment is made for the center of this system where the white-light fringes may be found. When the apparatus was first assembled on Mount Wilson, the time required for the approximate adjustment of the distances between mirrors with the wood rods was about one hour, for the centering of the mirrors fifteen minutes, for finding the fringes with sodium light thirty minutes, and for finding the fringes with white light forty-five minutes, or two hours and a half for the entire operation. Upon another occasion, the fringes for sodium light were found with ten minutes of searching and the white-light fringes in thirty-five minutes more. The mercury arc and other monochromatic sources have been tried for the preliminary adjustments but the sodium light is preferred because the middle portion of the interference system can be easily located, which corresponds to equal light paths in the two arms of the
interferometer. White-light fringes were chosen for the observations because they consist of a small group of fringes having a central, sharply defined black fringe which forms a permanent zero reference mark for all readings. Previous to 1924, a small acetylene lamp of the kind used on bicycles, was the source of light, the lamp being carried on a bracket attached to the end of one arm of the interferometer, as shown in Figs. 10 and 13. Such a lamp produces a concentrated brilliant and very steady light with the minimum production of heat and the lamp itself is very simple and of small weight and it burns for several hours with little attention. For the observations of 1924 and for part of the observations of April, 1925, the source was placed outside of the interferometer room, as is ex. plained later, and a larger lamp of the kind used for automobile headlights, shown in Fig. 14, was used. In April, 1925, the small acetylene lamp was again adopted, now being placed on the top of the cover of the interferometer, over the central axis, as shown in Fig. 16, the light being introduced into the light-path by two mirrors on the end of one arm. This arrangement has been continued to the present. Monochromatic fringes have never been used in the ether-drift observations, though experimental trials have been made, as is described later.

The interference fringes appear to be formed on the surface of the most distant mirror, optically speaking, No. 8, of the series as described. Attached to the supporting frame of this mirror is a small arrow-head of brass, which projects into the field of view, almost in contact with the mirror, forming a fixed fiducial mark for determining the position of the fringe system. Before beginning observations the end mirror, No. 8, on the telescope arm is very carefully adjusted to secure vertical fringes of suitable width. There are two adjustments of the angle of this mirror which will give fringes of the same width but which produce opposite displacements of the fringes for the same change in one of the light-paths. Very careful attention is required always to secure that adjustment of this critical angle which causes the arrow-head pointer to appear to the right of the central black fringe when the light-path of the telescope arm of the interferometer increases in effective length; a
reading for such a position is recorded as plus. When the pointer appears to the left of the central fringe the reading is minus, corresponding to a shortening of the telescope arm. The adjustment commonly employed is such that from six to ten fringes appear in the field of view and so that the central black fringe is never more than two fringe-widths from the pointer. Fig. 7 shows


Fig. 7. The interference fringes as seen in the interferometer.
the field of view with adjustments for narrow fringes and for wide fringes, the latter corresponding to the conditions of actual observation.

## Method of using the interferometer

The method of using the interferometer for the detection of an ether-drift presumes that the telescope arm of the instrument will be placed in the line of motion of the earth with respect to the ether as projected on the plane of the interferometer, while the other arm is at right angles to this motion. The interference fringes will indicate a certain reading with respect to the pointer in the field of view. The apparatus is then turned through an angle of azimuth of $90^{\circ}$ so that the effect of the earth's motion on the apparent velocity of light is transferred from the telescope arm to the other arm, with the result that the interference system will be displaced by an amount depending upon the square of the ratio of the velocity of the earth's absolute motion to the velocity of light. However, the direction of the earth's absolute motion is unknown and it is not possible to place the interferometer certainly in the desired positions. The interferometer is therefore caused to rotate slowly on the mercury float so that the telescope points successively to all azimuths. A relative motion of the earth and ether would then cause a
periodic displacement of the interference fringes, the fringes moving first to one side and then to the other as referred to the pointer in the field of view, with two complete periods in each rotation of the instrument.

Uniform temperature conditions are important as regards the dimensions of the apparatus and the refraction of the air in the light path. Usually the apparatus is kept in motion for an hour or more before readings are begun; sometimes a fan is used to secure uniform temperature distribution and the opening of the windows on all sides is common. However, when observations are made in daylight, the windows must be covered with curtains or dark paper. The apparatus is set in rotation by a pull of a few ounces on a fine string attached to the wooden float; a moderate pull on this string, even up to its breaking point, does not produce any appreciable distortion in the steel interferometer which rests on the float. The interferometer turns so easily and has such inertia that when once started it will continue to turn for an hour and a half or more without any further pull or push. It rotates with such freedom that it is literally "floating" without acceleration or distortion.

The purpose of the observation is to determine the amount of the displacement of the fringes and the direction in which the telescope points when this displacement is a maximum. The observer has to walk around a circle about twenty feet in diameter, keeping his eye at the moving eyepiece of the telescope attached to the interferometer which is turning on its axis steadily, at the rate of about one turn in fifty seconds; the observer must not touch the interferometer in any way and yet he must never lose sight of the interference fringes, which are seen only through the small aperture of the eyepiece of the telescope, about a quarter of an inch in diameter. The string attached to the float, mentioned above, may be used as a sensitive guide to assist the observer in maintaining the proper circular path. A delicate metal brush attached to the wood float touches in succession sixteen equidistant contact pieces on the mercury tank, closing an electric circuit which operates a small sounder and indicates the instants at which readings are to be made.

It is entirely practicable to make the readings
of the positions of the interference fringes corresponding to the sixteen equidistant azimuths of one complete turn of the interferometer when the instrument is turning at the rate of one turn in about fifty seconds. A "set" of readings which corresponds to a "single observation," represented by one point on the charts of the original observations, usually consists of twenty turns, involving three hundred and twenty readings, made in about eighteen minutes. The time midway between the beginning and ending of the set of readings is taken as the time of the observation. The twenty turns are ordinarily observed in continuous succession; however, if a single reading at any one azimuth is lost, due to vibration of the support or other cause, the entire turn is cancelled. The adjustments are maintained so that the central fringe of the field of view, Fig. 7, is never more than two fringewidths from the fiducial point. Often the temperature drift is such that the fringes shift more than this before a set of twenty turns is completed. When this occurs, the fringe system is restored to its central position simply by placing a small weight of two or three hundred grams on the end of the arm or by removing a weight from the arm. This is done without stopping the uniform turning of the apparatus and usually without interrupting the readings; if a reading is lost, the entire turn is cancelled and the observations are continued until twenty complete turns of readings have been secured. Only rarely is it necessary to readjust the fringes by means of the screws against which the end mirror rests. On some occasions the temperature conditions are so steady that no adjustment of fringes is required through several sets, which may cover an interval of an hour or more. Such sets of observations are repeated continuously during the several hours of the working period.
It is considered very important that the interferometer should not be enclosed in a metallic casing, nor even in an opaque covering; also that it should not be placed inside a room with heavy walls such as are required for a constant-temperature room. The apparatus should be, as nearly as possible, in the open so that there is no possibility of entrainment of the ether in massive materials surrounding it. The instrument is very sensitive to changes of
temperature and to vibration of the support and the quantity to be measured is extremely small. When the apparatus is used with the least possible covering, it is subjected to greater temperature disturbances than when fully protected, which results in greater dispersion among the separate readings; it is therefore necessary to accumulate a larger number of readings as rapidly as possible under these conditions and to arrange and combine them in such a manner that the systematic ether-drift effect will be fully preserved while the temperature changes which proceed more slowly will be eliminated in the final average. As the readings are taken at intervals of about three seconds, the position of the maximum displacement is dependent upon readings covering an interval of less than ten seconds. A complete period of the displacement takes place in about twenty-five seconds. Any temperature effect or other disturbing cause which is not strictly periodic in every twenty-five seconds over an interval of fifteen minutes would largely be cancelled out in the process of averaging, while a real periodic effect persists. Thus the observations for the direction of the absolute motion are largely independent of ordinary temperature variations. The observation is a differential one and can be made with considerable certainty under all conditions. Disturbances, due to temperature or other causes lasting for a few seconds or for a few minutes, might affect the actual amount of the observed displacement and give less certain values for the velocity of the ether-drift while, at the same time, the position of maximum displacement is not altered.
Previous to 1925, the time of actual readings had been confined to one or two hours at a predetermined time of day; the time required for preparation and preliminary adjustments would perhaps be two hours more. The procedure adopted in 1925 makes it necessary to have observations equally distributed over the twenty. four hours of the day to determine the curve of diurnal variation. Allowing a few minutes for reading thermometers and for making readjustments of fringes and also a few minutes for relaxation, two sets of readings may be made in each hour through a working day, or night, of eight hours. The accumulation of a hundred sets
of readings, distributed over the twenty-four hours of the day will, under favorable weather conditions, occupy a period of six or eight days. Such a series of observations is finally reduced to one group, corresponding to the mean date of the epoch; several series of this extent are represented in Fig. 22.
The observer has only one single thing to do, that is to note and announce the position of the central black fringe with respect to the fiducial point, plus or minus, in units of a tenth of a fringe width, at the instant of the click of the electric sounder. An assistant records these readings in order, on a prepared form, starting with the reading corresponding to the north or other noted azimuth, as shown in Fig. 8, which is the


Fig. 8. Form of record of ether-drift observations.
record of actual observations made at Mount Wilson on September 23, 1925. The observer gives no attention to the azimuth. The reading is determined by instantaneous visual estimation; it is quite impracticable to use any kind of a scale in the field of view because the width of the fringes is subject to slight variation. That this


Fig. 9. Interferometer readings and the process of reducing them for the ether-drift effect.
method is sufficient is shown by the uniformly consistent and systematic periodic curves representing the observations. The numerical quantity used as the result of a "single observation" is the average of forty such readings (the function being periodic in each half-turn) and it approaches an accuracy of a hundredth of a fringe.

While readings are being taken, neither the observer nor the recorder can form the slightest opinion asato whether any periodicity is present, much less as to the amount or direction of any periodic effect; the taking of observations is quite unprejudiced and is simply mechanical. That this must be true will be evident from an inspection of the numbers representing the readings as recorded in the chart, Fig. 8, and shown graphically in Fig. 9.

## Reduction of the interferometer observations

The numerical reduction of a set of readings is a simple arithmetical process. In the record, Fig. 8, the horizontal lines give the sixteen readings for one turn of the interferometer, the first reading being that when the telescope points to the north; the readings for twenty turns are shown. The seventeenth number at the end of each line is the first reading of the next succeeding line or turn; if an adjustment of fringes is made, this number is for the beginning of the next turn, before the adjustment is made. The twenty numbers in each column are added with respect to the plus and minus values. Under ideal conditions, all the numbers in column one (and in column seventeen) should be the same integer but actually there is always some shift of the fringe system with respect to the fiducial point. This shift is assumed to be steady, or linear, throughout the time of one turn, about twenty-
five seconds, which is equivalent to assuming that the periodic displacements of the fringes take place with respect to an inclined axis. A compensation for the shift is made by adding to the sum of the seventeenth column such a number as will make it equal to the sum of the first column and by adding one-sixteenth, twosixteenths, etc. of this compensating number to the second, third, etc. columns; this renders the axis of reference horizontal. These compensated sums of the sixteen columns of readings are divided by twenty, the number of turns of recordings, giving the average positions of the central black interference fringe for each of the sixteen azimuths of one complete turn around the horizon. The mean ordinate is now subtracted from the ordinate of each point and these points, plotted, will give the curve of fringe displacement referred to its own time axis.

In the definitive study of the ether-drift effect, this set of sixteen average readings for the position of the interference fringes is plotted to a large scale and is subjected to mechanical harmonic analysis to evaluate precisely the second harmonic component, which represents the second-order, half-period ether-drift effect; this process is illustrated in Fig. 21 in a later section. For the purpose of a preliminary study of the observations, it is convenient to obtain an approximate graphic representation of the effect by the following procedure. The second half of the line of sixteen average readings is placed under the first half and the mean of the two numbers in each column is obtained; by this addition any periodic full-period effect is eliminated and also any effect of all higher odd harmonic components. The final line of eight numbers represents the mean values of the ordinates of the half-period effect, together with higher even harmonics which may be present, obtained from forty sets of readings of this second-order effect. At the bottom of the chart, Fig. 8, are plotted the readings for the full turn of the interferometer, which contain all the effects observed and below this the readings for the half-period effects.

The set of readings here illustrated is not exceptional; it is a fair sample as to magnitude and periodicity of the ether-drift effect. This particular displacement corresponds to an ether-
drift velocity of 9.3 kilometers per second. Every set of readings shows a very definite periodicity which varies both as to magnitude and phase ina systematic manner.

The method of reducing the observations is further illustrated by the graphic representation of Fig. 9 which shows the complete process as applied to the first five turns of the record given in Fig. 8. The readings for the five turns are plotted to scale at the top of the figure. Below this at the left is shown the summation of the five turns for the sixteen azimuths of one complete turn in which the periodic displacements clearly oscillate about the downwardly inclined axis, below this are the linear compensations for the shift and next below this the sums of the readings with the shift eliminated. The mean of the sixteen ordinates is subtracted from each ordinate, giving the curve referred to its own true axis, as shown at the right. Below this are shown the two halves of the full-turn curve, one. below the other; still lower is the half sum of the two curves, from which the full-period effect is now eliminated. This is the average effect for the half period obtained from the sum of the five turns; for final evaluation the ordinates are to be divided by five; this is indicated by a change of scale in the figure. It is interesting to note that the full-turn and the half-turn curves obtained from the readings for five turns are almost identical with the corresponding curves obtained from the full set of readings for twenty turns shown in Fig. 8.

## Stability of the interferometer

The steel cross which forms the base of the interferometer has proved to be remarkably stable and dependable. The length of the light path, going and returning, is about $112,000,000$ wave-lengths and, for the production of the interference fringes in white light, the two light paths, which are at right angles to each other and each of which consists of sixteen separate parts, must be exactly equal to the fraction of a wave. length. A difference in length of from five to ten wave-lengths displaces the white-light interference system so much that it is no longer visible in the telescope when the adjustment is made for wide fringes. The screws used for thi adjustment of the end mirror, No. 8, hav
threads 0.635 millimeter apart, and a turn of the screw through $16^{\circ}$ causes a change of 100 wavelengths in the light path. These screws are turned by means of capstan pins in order to secure sensitive adjustment. Usually the final adjustment of the central fringe to the fiducial point is secured by means of small weights placed on the end of the arm of the cross, causing a change of length by flexure.
Tests have been made at various times to determine the rigidity of the steel cross; these show that the four arms are about equally rigid and that a weight of 282 grams placed on the end of one arm produces an elongation in the multiple light-path sufficient to displace the fringe system one fringe-width, which is less than one hundred-millionth part of the light path. Similar tests made on the concrete base used for the interferometer in December, 1924, showed that 30 grams on the end of the arm produce a displacement of one fringe-width; the concrete base was therefore nearly ten times as sensitive to distortion as is the steel.
A change in temperature of the apparatus as a whole causes a slight change in the relative lengths of the arms. The white-light fringes having been adjusted to the center of the field of view, a change in temperature causes the fringes to be displaced out of view ; however, the change is quite reversible and a return to the first temperature brings the fringes again into view. It has occurred repeatedly that at the close of a day's work the fringes would be in the field of view and upon returning the next day, after the drop and rise in temperature of the night, the fringes would be in the field without any readjustment. The temperature influence on the apparatus is so consistent that a scale of temperature is provided for the capstan pin of the adjusting screws. A change of $10^{\circ}$ in temperature requires a change of about $18^{\circ}$ in the turning of the screw, corresponding to a displacement of 112 wave-lengths in the double light-path.
The sodium light is used in making the adjustments when the apparatus is first assembled at the beginning of a series of observations. After the white-light fringes have been lound these are rarely lost and it is not necessary to resort to the monochromatic light again during the entire period of observations, unless the
apparatus is disassembled for some cause. The white-light fringes have been kept in adjustment during a period of two weeks or more. Upon the completion of observations at Mount Wilson in September, 1925, the mirrors and other optical parts were removed and packed for safekeeping. When observations were resumed in February, 1926, the mirrors were repolished and all parts were reassembled; the fringes in white-light were found in less than one minute without the use of the sodium light.

Since 1927, the interferometer has been mounted on the campus of Case School of Applied Science, about 330 feet from Euclid Avenue; the passage of street cars and the motor traffic of the city thoroughfare do not interfere with the making of observations. However, it is interesting to note that the sound of the imperfectly muffled exhaust of a motor-truck or a motorcycle, which may be a thousand feet or more distant, will cause the fringes to disappear completely without the slightest tremor. When observations were being made on the Fourth of July, 1904, the discharge of large fire crackers twelve hundred feet distant, produced the same effect. This is due not to mechanical vibration, but to the passage of the sound waves through the air in the light path of the interferometer. On several occasions in the observations made at Mount Wilson, there were minute but very distinct seismic disturbances which for a few seconds completely obliterated the fringes. After one such "earthquake," or micro-seismism, it was necessary to readjust the end mirror through a distance of twenty wave-lengths. A man chopping a stump of wood, several hundred feet away, disturbed the fringes, as also did workmen on a highway three miles distant; the passing of an airplane overhead caused the disappearance of the fringes.

## Observations by Morley and Miller in 1904

The interferometer with the steel-girder base was first used by Morley and Miller in a continuance of the test of the Lorentz-FitzGerald contraction hypothesis. For this purpose the mirrors were so mounted that the distances between them could be made to depend upon the lengths of rods of pine wood. On two ends of the cross, $S$ and $T$, Fig. 6, are two upright frames of


Fig. 10. The Morley-Miller ether-drift interferometer arranged for tests of the Lorentz-FitzGerald hypothesis, 1904.
cast iron, fastened by bolts; each frame carries four mirrors. Against the corners of each of these frames rest four pine rods, about 2 centimeters in diameter and 425 centimeters long. Each rod is supported throughout its length by a brass tube, 2.5 centimeters in diameter, and each pair of tubes is joined together in a vertical truss, as shown in Fig. 10. Against the farther ends of the wood rods, rest the frames which hold the other sets of mirrors. Each of the latter frames is freely suspended by two thin steel ribbons and is held firmly against the pine rods and through these against one of the two fixed mirror-holders; contact is maintained by means of adjustable spiral springs. Thus the distances between the opposite systems of mirrors depend upon the pine rods only, while the whole optical system is adequately supported by the steel cross.
The first observations with this apparatus were made in July, 1904, and consisted of 260 turns of the interferometer arranged in two series. The procedure was based upon the effect to be expected from the combination of the diurnal and annual motions of the earth, together with the presumed motion of the solar system towards the constellation Hercules. On the dates chosen for the observations there were two times of the day when the resultant of these motions, about 33.5 kilometers per second, would lie in the plane of the interferometer, 11:30 o'clock, A.m., and 9:00 o'clock, P.M. The calculated azimuths of the motion would be different for
these two times but the velocities would be the same and the observations at these two times were, therefore, combined in such a way that the presumed azimuth for the morning observations coincided with that for the evening. The observations for the two times of day gave effects having positive magnitudes but having nearly opposite phases; when these were combined, the half sum was nearly zero. This small result was opposed to the theory then under consideration and it seemed impossible to reconcile the observations with the known orbital motion of the earth. The report of these experiments, published in the Philosophical Magazine, ${ }^{9}$ in May, 1905, concludes with this statement: "If pine is affected at all as has been suggested, it is affected to the same amount as is sandstone, Some have thought that this experiment only proves that the ether in a certain basement room is carried along with it. We desire, therefore, to place the apparatus on a hill to see if an effect can be there detected." The two curves for the ether. drift obtained from the morning and the evening observations of July, 1904, are shown in Fig. 11 , being superimposed, as explained above; the lower curve represents the mean displacement thus obtained, which is the result given in the published account of these experiments.

In accordance with the results set forth later in this report, this procedure of 1904 was incorrect,

[^5] (1905); Proc. Am. Acad. Sci. 41, 321 (1905).


Frg. 11. Method of combining the ether-drift observations of July, 1904, now considered erroneous.
being based upon an erroneous hypothesis as to the resultant absolute motion of the earth. The morning and evening observations each indicate a velocity of ether drift of about 7.5 kilometers per second; these values are charted in Fig. 4 in relation to the magnitudes predicted by the new hypothesis of a much larger predominating cosmic motion of the solar system and show reasonable consistency.

## Observations by Morley and Miller in 1905

In 1905, the interferometer was mounted in a temporary hut on a site in Cleveland Heights, free from obstruction by buildings and at an altitude of about 285 meters. The house was provided with glass windows at the level of the interferometer so that there should be no opaque screens in the plane of drift. The test of the contraction hypothesis was continued; the wooden rods which determined the length of the optical path in the experiments of 1904 were omitted and all the mirror frames were fastened to the steel base, so that, for contrast, the optical distances were now determined by the steel. The program alsso included an investigation of an ether drift with the apparatus at the higher devation and free from obstruction by buildings. The observations made here in July, October and November, 1905, consisting of 230 turns in three sets, showed a very definite positive effect slightly larger than that previously obtained, but still too small to be reconciled with the expectation. The velocity of relative motion of the
earth and ether obtained from the observations made in October is 8.7 kilometers per second; this is shown on the chart, Fig. 4; as compared with the result to be expected from the new theory here presented, the agreement is almost perfect. Plans were made for testing various modifications of theory but before these were carried out circumstances beyond control required that the interferometer be dismounted. Professor Morley retired from active service and it devolved upon the writer to continue the experiments. It seemed desirable that further observations should be carried out at a much higher altitude but several causes prevented the immediate resumption of the work. Other interests developed and though the expectation of continuing the experiments persisted, a long delay ensued.

## The Inception of the Theory of <br> Relativity, 1905

The Theory of Relativity had its inception at this time when Einstein published his paper entitled Zur electrodynamik bewegter Körper, in November, $1905,{ }^{10}$ and was elaborately developed in succeeding years. The tests of the theory of relativity, made at the solar eclipse of 1919 , were widely accepted as confirming the theory. Since the Theory of Relativity postulates an exact null effect from the ether-drift experiment which had never been obtained in fact, the writer felt impelled to repeat the experiment in order to secure a definitive result. An elaborate program was prepared and ample funds to cover the very considerable expense involved were very generously provided by Mr. Eckstein Case of Cleveland.

## The Mount Wilson Experiments, 1921

## Observations of April, 1921. Steel interferometer

Through the courtesy of the Carnegie Institution of Washington, the ether-drift interferometer was set up on Mount Wilson in March, 1921, on the grounds of the Mount Wilson Observatory, on Rock Crusher Knoll or "Ether Rock" as it came to be called, near the site of the 100 -inch telescope, at an altitude of about 1750 meters. A concrete foundation was laid on the bare rock of

[^6]the knoll and four concrete piers were formed to support the iron mercury tank at a suitable height. This was enclosed in a light housing, Fig. 12, twenty feet square and about twelve feet high at the ridge of the roof. The sides of the house were enclosed with sheets of corrugated


Fig. 12. Interferometer house on "Ether Rocks," Mount Wilson.
iron, except that at a height of from four to seven feet above the floor, on all sides there were continuous "windows" of white canvas cloth. The canvas was attached to a series of frames so that the windows could be opened on all sides at the level of the interferometer, for a width of three feet. In the south end was a small door with iron and canvas panels to match the sides of the house. A rough flooring was placed a little above the rock; on this floor a smooth circular track was constructed on which the observer could walk comfortably while following the interferometer as it turns slowly on its axis. This house was purposely constructed with wide cracks at the various joints in the sides and floor and under the eaves, so that there should be a very free circulation of air to secure equalization of temperature with the outside air. The opening of the windows on all sides greatly facilitated this condition. In order to secure sufficient darkness for the observation of the fringes in the daytime, sheets of thin black paper were placed over the canvas windows and over such holes and cracks as admitted too much light. Electric current was supplied to the house and several fixed and portable lamps were available. Common and
precision thermometers were hung on each side of the house and were read at the beginning and end of each set of observations. A barograph and a thermograph were carried at all times on the interferometer itself. An anemometer was attached to the roof of the house. A copy of the Mount Wilson Observatory meteorological records was also secured for the duration of the observations. These general arrangements apply to all subsequent experiments.

Observations were begun on April 8 and continued till April 21, 1921, by means of the apparatus and methods employed by Morley and Miller in 1904 and 1905, with certain modif. cations and developments in details. The first observations of sixty-seven sets consisting of 350 turns gave a positive effect such as would be produced by a real ether-drift, corresponding to a relative motion of the earth and ether of about ten kilometers per second. Before announcing such a result, it seemed necessary to study every possible cause which might produce a displacement of fringes similar to that caused by etherdrift; among the causes suggested were radiant heat, centrifugal and gyrostatic action, irregular gravitation effects, yielding of the foundation, magnetic polarization and magnetostriction. In order to test the first, the metal parts of the interferometer were completely covered with cork about one inch thick, and fifty sets of observations consisting of 273 turns were made; there was a periodic displacement of the fringes, as in the first observations, showing that radiant heat is not the cause of the observed effect.

## Observations of December, 1921. Concrete interferometer

In the summer of 1921, the steel frame of the interferometer was dismounted and a base of one piece of concrete, Fig. 13, reinforced with brass, was cast in place on the mercury float. All the metal parts which were supported on the concrete base were made of aluminum or brass. The entire apparatus was free from magnetic effects and the possible effects due to heat were much reduced In December, 1921, forty-two sets of observations, consisting of 422 turns, were made with the nonmagnetic interferometer. These show a positive effect as of an ether drift, which is


Fig. 13. Interferometer with base of concrete, 1921.
entirely consistent with the observations of April, 1921.

Many variations of incidental conditions were tried at this epoch. Observations were made with the centering pin tight in its socket and then lose; with rotation of the interferometer clockwise and counterclockwise; with a rapid rotation of one turn in 40 seconds and a slow rotation of one turn in 85 seconds; with a heavy weight added first to the telescope arm of the main frame and then to the lamp arm; with the float extremely out of level because loaded first in one quadrant and then in the next quadrant; with the recording assistant walking round in different quadrants and standing in different portions of the house, near to and far from the apparatus.

The results of the observations were not affected by any of these changes.

It was demonstrated that the use of the concrete base did not change the effect observed with the steel base either in magnitude or azimuth. The concrete base was less affected than the steel by change of dimensions due to changes of temperature; but this slight advantage was counterbalanced by the fact that it accommodated itself more slowly to a change of temperature. In spite of the fact that the concrete was considerably heavier than the steel parts which it displaced, it was much less rigid. Tests showed that a weight of 30 grams placed on the end of the arm of the interferometer would produce a displacement of the fringes of one fringe width, while nearly ten times as much weight is required to produce the same effect with the steel base. The concrete base was abandoned and the original steel base has been used in all subsequent observations.

## Laboratory Tests of the Interferometer, Cleveland, 1922-1924

The entire apparatus was returned to the laboratory at Cleveland; during the years 1922 and 1923 many trials were made under various conditions which could be controlled and with many modifications in the details of the apparatus. An arrangement of mirrors and prisms was made so that the source of light could be placed outside of the observing room, Fig. 14, the


Fig. 14. The interferometer in the laboratory, 1923.
light entering the rotating interferometer along the axis of rotation. A further arrangement of mirrors, rather complicated in practice, was tried, for observing the fringes from a stationary telescope; the necessity for frequent adjustment of the fringes in the field of view made this method impracticable. Experiments were made with devices for the photographic registration of the positions of the fringes, both from the fixed observing station and by means of a motion picture camera carried on the interferometer. Even with an arc light as the source, there was not sufficient illumination to produce a satisfactory photographic record without slowing the rotation of the apparatus more than is consistent with our method of procedure, and the necessity for frequent adjustment of the fringes also made this method unsuitable. After abandoning the photographic method, an astronomical telescope having an objective of 13 centimeters aperture and a focal length of 190 centimeters was mounted on the interferometer. The objectglass is attached to the steel base near the halfsilvered diagonal glass and the eyepiece is supported on the end of the arm, there being no tube for the telescope. With a magnification of fifty diameters, the fringes are observable on a large scale and with ample illumination, so that direct reading with the eye was very satisfactory; this arrangement has been used in all subsequent observations.
Trials were made with various sources of light; with electric arc and incandescent lamps, the mercury arc, acetylene lamp and also with sunlight. The interchange between sunlight and laboratory sources in no way altered the results. The final choice for the stationary source placed outside of the interferometer room (or house, on the mountain) was a large acetylene lamp of the kind commonly used for automobile headlights. This arrangement was used in Cleveland in 1924 and at Mount Wilson in September, 1924, and in April, 1925. The use of a stationary light source with the light brought to the interferometer in the axis of rotation required very careful adjustment of the several mirrors involved in order to avoid a periodic displacement of fringes due to non-axial alignment. Careful trials were made which showed that it was better to place the source on the interferometer outside of the
cover and near the axis; thus the relation source to the instrument remained constant When this method was adopted, the sma acetylene lamp, such as was used in the earlie experiments, was employed. This method illumination has been used exclusively sinc April 9, 1925.

An extended series of experiments was madet determine the influence of inequality of tempera ture in the interferometer room and of radian heat falling on the interferometer. Several electri heaters were used, of the type having a heate coil near the focus of a concave reflecto Inequalities in the temperature of the roor caused a slow but steady drifting of the fring system to one side but caused no period displacement. Even when two of the heater placed at a distance of three feet from th interferometer as it rotated, were adjusted throw the heat directly on the uncovered ste frame, there was no periodic effect that $w$ measurable. When the heaters were directed the air in the light-path which had a covering glass, a periodic effect could be obtained on when the glass was partly covered with opaq material in a very nonsymmetrical manner, when one arm of the interferometer was con pletely protected by a covering of corrugat paper-board while the other arms were unpr tected. These experiments proved that under t conditions of actual observation, the period displacements could not possibly be produced temperature effects.

## The Mount Wilson Experiments, 1924

Upon the conclusion of the experiments ju described, in July, 1924, the interferometer w. taken again to Mount Wilson. In 1921 apparatus had been located on the very edge of deep canyon; it was feared that the air curren up and down the face of the canyon mig produce a disturbance and also that the unsyl metrical distribution of the rock of the mounta itself might be undesirable. In August, 1924, new site was chosen on a very slightly rounde knoll, removed from the canyons. The inte ferometer house, Fig. 15, was erected with orientation, as regards the ridge of the roof an the location of the door, changed by $90^{\circ}$


Fig. 15. Ether-drift house at Mount Wilson in 1924-1926.
that of 1921. The house was about twenty-two feet square, and there were canvas windows all around as before; but instead of the corrugated iron for the sides, beaver-board was used, as this material is less absorbent of heat from the sun. Large pieces of canvas were placed over the entire house and at the end, to protect the house from the direct rays of the sun, greatly facilitating the making of observations throughout the period of daylight. The interferometer, Fig. 16, had the improved mirror mountings, protection from heat, improved light-source, large viewing telescope and other refinements which had been developed in the laboratory tests at Cleveland in 1923 and 1924.
This series of observations, of September, 1924, at Mount Wilson, was undertaken in a wholly unprejudiced but very confident state of mind. The extended laboratory tests had involved every suggested source of instrumental and external disturbance and had proved that none of these was operative in the experiment. The method of observing was so developed that there was perfect confidence in the readings. It was


FIg. 16. The ether-drift interferometer as used at Mount Wilson in 1924-1926.
felt that if any of the suspected disturbing causes had been responsible for the previously observed effects, now these were removed, the result would be a true null effect. Such a conclusion would have been accepted with entire satisfaction; and indeed it was almost expected. On the other hand, if the observations continued to give the positive effect, it would certainly have to be considered as real.

Ten sets of readings, consisting of 136 turns. of the interferometer, were made on September 4, 5 and 6, 1924. These observations all show a positive periodic displacement of the interference fringes, as of an ether-drift, of the same magnitude, about ten kilometers per second, as had been obtained in previous trials. Part of these observations were made with the glass case over the light-path covered with corrugated paper board, which had been found in the Cleveland experiments to exclude all effects of radiant heat; the results were not altered in any way by this covering. The effects were shown to be real and systematic, beyond any further question.
In spite of the long continued efforts, it had so far been impossible to account for the effects observed in the interferometer as being due to terrestrial causes or to experimental errors. Very extended calculations were made in the effort to reconcile the observed effects with the accepted theories of the ether and of the presumed motions of the earth in space. The observations had been repeated at various epochs to test one after another of the hypotheses which had been suggested. At the end of the year 1924 when a solution seemed impossible, a complete calculation was made, for all hours of the day and for twenty-four epochs during the year, of the then expected effects due to the orbital motion and the apparent motion towards Hercules. This indicated that the effect to be expected had its greatest magnitude in April and that the minimum in April should be two and a half times as great as the effect at the time of the observations which had been made in September and that the maximum effect in April should be four and a half times as great. Furthermore, the effect in September would be directed to the northward at all times of the day while in April the azimuth of the effect would move progressively all around the horizon, the maximum value being attained
at midnight with a direction exactly east and again at noon with a direction exactly west. Observations for verifying these contrasting predictions were made at Mount Wilson between March 27 and April 10, 1925. The effect was equal in magnitude to, but not larger than, the effects previously observed; it was not directed successively to all points of the compass, that is, it did not point in directions $90^{\circ}$ apart at intervals of six hours. Instead of this, the direction merely oscillated back and forth through an angle of about $60^{\circ}$, having, in general, a northerly direction, as before. This proved that the presumptions as to the absolute motion of the earth, upon which these calculations were based, were invalid.

## General Analysis of the EtherDrift Problem

## The various component motions involved

Previous to 1925, the Michelson-Morley experiment had always been applied to test a specific hypothesis. The only theory of the ether which had been put to the test is that of the absolutely stationary ether through which the earth moves without in any way disturbing it. To this hypothesis the experiment gave a negative answer. The experiment was applied to test the question only in connection with specific assumed motions of the earth, namely, the axial and orbital motions combined with a constant motion of the solar system towards the constellation Hercules with the velocity of about nineteen kilometers per second. The results of the experiments did not agree with these presumed motions. The attention was given almost wholly to this velocity of the ether drift, and no attempt was ever made to determine the apex of any indicated motion. The experiment was applied to test the Lorentz-FitzGerald hypothesis that the dimensions of bodies are changed by their motions through the ether; it was applied to test the effects of magnetostriction, of radiant heat and of gravitational deformation of the frame of the interferometer. Throughout all these observations extending over a period of years, while the answers to the various questions have been "no," there has persisted a constant and consistent small effect which has not been explained.

The ether-drift interferometer is an instrument which is generally admitted to be suitable for determining the relative motion of the earth and the ether, that is, it is capable of indicating the direction and the magnitude of the absolute motion of the earth and the solar system in space. If observations were made for the determination of such an absolute motion, what would be the result, independent of any "expected" result? For the purpose of answering this general question, it was decided to make more extended observations at several epochs when the earth is in contrasting positions in its orbit and this was done in the months of April, August and September, 1925, and in February, 1926.

It may be asked: why was not such a procedure adopted before? The answer is, in part, the fact already stated that the purpose had been the verification of certain predictions of the so-called classical theories; and, in part, that it is not easy to develop a new hypothesis, however simple, in the absence of direct indication. Probably a considerable reason for the failure is the great difficulty involved in making the observations at all times of day at any one epoch. Very few, if any, scientific experiments require the taking of so many and continuous observations of such extreme difficulty; it requires greater concentration than any other known experiment. Half the time, perhaps, the observations are interrupted before they become numerous enough to be useful, because of excessive displacement of the fringes by temperature changes or by earth or aerial vibrations. The mere adjustment of an interferometer for white-light fringes and the keeping of it in adjustment, when the light path is 210 feet long, made up of sixteen different parts, and when it is in effect in the open air, requires patience as well as a steady "nerve" and a steady hand. Professor Morley once said, "Patience is a possession without which no one is likely to begin observation of this kind."

The absolute motion of the earth may be presumed to be the resultant of two independent component motions. One of these is the orbital motion around the sun, which is known both as to magnitude and direction. For the purposes of this study, the velocity of the orbital motion is taken as 30 kilometers per second and the
direction changes continuously through the year, at all times being tangential to the orbit. The second component is the cosmical motion of the sun and the solar system. Presumably this is constant in both direction and magnitude but neither the direction nor magnitude is known; the determination of these quantities is the particular object of this experiment. The wellknown motion of the solar system towards the constellation Hercules, with a velocity of 19 kilometers per second, is only a relative motion of the sun with regard to the group of nearby stars and it may give no information as to the motion of the group as a whole. In fact, the previous ether-drift experiments have clearly shown that the motion towards Hercules is not a component of the absolute motion of the earth. The rotation of the earth on its axis produces a velocity of less than four-tenths of a kilometer per second in the latitude of observation and is negligible as far as the velocity of absolute motion is concerned; but this rotation has an important effect upon the apparent direction of the motion and is an essential factor in the solution of the problem. However, since the orbital component is continually changing in direction, the general solution is difficult; but by observing the resultant motion when the earth is in different parts of its orbit, a solution by trial is practicable. For this purpose it is necessary to determine the variations in the magnitude and in the direction of the ether-drift effect throughout a period of twentyfour hours and at three or more epochs of the year.
The interferometer continually rotates in a horizontal plane about a vertical axis at the latitude of the observatory. As the earth rotates on its axis, the axis of the interferometer extended may be considered as the generating element of a cone, the apex of which is at the center of the earth. The earth in its orbital motion carries this cone around the orbit, the axis of the cone, the earth's axis, always pointing in the same direction in cosmic space. At the same time this system with rotations about three different axes is being translated through space in an unknown manner. It is presumed, further, that the ether-drift interferometer will detect only that single component of the complicated combination of translations and rotations which
at the instant lies in the optical plane of the interferometer; it gives the magnitude and direction of this one component. Fig. 17 shows a globe with a model representing an interferometer attached at a point corresponding to Mount Wilson. The wire extending from the pole of the globe indicates the direction of an assumed


FIg. 17. Models illustrating the diurnal variation in the magnitude and direction of the ether-drift effect.
resultant absolute motion. With the earth in the position shown in the left view, the projection of the motion indicated by the wire, on the plane of the interferometer, passes through the north and south points and has a magnitude less than the full value of the motion. When the earth has turned on its axis to the position shown in the middle view, the projection of the absolute motion in the plane of the interferometer lies to the west of north; as the interferometer rotates on its axis the telescope will detect the maximum component when it points west of north. When the earth has turned to the position shown at the right, the projected component of motion will again be north and south and will have a maximum value, slightly less than the full value. Thus there is a diurnal variation in the observed azimuth of ether-drift. It is evident, further, that the angle which the absolute motion makes with the plane of the interferometer varies throughout the day as the interferometer is carried around on the cone described by its axis. In the illustration, the absolute motion most nearly coincides with the plane of the interferometer in the right view which corresponds to a maximum observed effect; in the left view, the motion is more nearly perpendicular to the plane of the interferometer and the effect is a minimum. It follows that there is a diurnal variation in the magnitude of the effect and this is quite independent of the


Fig. 18. Model for studying the components of ether-drift.
azimuth variation, except insofar as they may be produced by one cause.

The model showri in Fig. 18, was prepared to assist in a study of the ether-drift effect in its astronomical relations. The large circular disk represents the plane of the interferometer which can be rotated around the inclined polar axis, bringing its plane into all the possible diurnal positions, corresponding to the Mount Wilson location. At the center of the disk is mounted a parallelogram whose sides can be made to represent any assumed values for the two components of the absolute motion, while the directions can be set as desired and the corresponding resultant will be reproduced. A small electric lamp is so supported that, as the inter-


Fig. 19. Model illustrating the diurnal variation in the azimuth of the ether-drift.
ferometer is rotated around the polar axis and while the parallelogram remains stationary, the lamp casts the shadow of the resultant on the plane of the interferometer, showing how the azimuth of the drift varies with the time of day. The angle which the resultant makes with the plane can be observed and thus the variation in magnitude of the drift for the assumed motion is determined. A probable value for the cosmical component of motion having been selected, a single wire representing the resultant for any epoch is substituted for the parallelogram and the diurnal variations in azimuth and magnitude are studied. Three views of the model, Fig. 19, show how the azimuth swings to the west of north and then to the east, for the motion assumed.

It is evident from these models that the observed ether-drift effect would be very different for different resultant motions, as for different epochs, and that it would vary greatly in different latitudes. The conditions shown correspond approximately to the results here to be considered.

## Solution for the absolute motion of the solar system

The point on the celestial sphere towards which the earth is moving because of its absolute motion is called the apex of its motion. This point is defined by its right ascension and declination, as is a star, and the formulae of ${ }^{\circ}$ practical astronomy are directly applicable to its determination from the interferometer observations. The theoretical consideration of the determination of the apex of the motion of the earth has been given in a paper by Professor J. J. Nassau and Professor P. M. Morse, which appeared in the Astrophysical Journal for March, 1927. ${ }^{11}$
Knowing the latitude of the observatory, $\phi_{\text {, }}$ and the sidereal time, $\theta$, of the observation, two independent determinations may be obtained for the right ascension, $\alpha$, and for the declination, $\delta$, of the apex of the earth's absolute motion, one determination from the observed velocity, $V$, and one from the azimuth, $A$, of the ether-drift effect. The ether-drift effect being a second order effect, periodic in each half turn of the apparatus,

[^7]it follows that if a certain magnitude of effect is observed when the telescope points in a given direction, exactly the same effect will be obtained when the interferometer has been rotated $180^{\circ}$ and the telescope points in the opposite direction. The interferometer observations determine the line in which the motion takes place but do not distinguish between the plus and minus directions of the motion in this line; the choice between the plus sign, northward, and the minus sign, southward, must be determined from the consistency of the result when this motion is combined with the known orbital motion of the earth. For simplicity in the presentation of the formulae, they will be given for an apex having a north declination and for an observatory located in the northern hemisphere. If the final solution requires a motion to the southward, the new apex will be diametrically opposite the one first determined; its right ascension will be the right ascension of the first apex minus 12 hours and its declination will have the same numerical value as that for the first apex but with the minus sign. For an observatory located in the southern hemisphere there would be certain systematic differences in the formulae which need not be given here.
The apex of the absolute motion determined from the magnitude of the ether-drift effect
It is shown in the paper by Nassau and Morse, what is also evident from a study of the model, Fig. 17, that the sidereal time, when the component of motion in the plane of the interferometer is a minimum, $\theta_{v=\text { min }}$, measures the right ascension of the apex; that is
$$
\alpha=\theta_{v=\min }
$$

It is evident that the component of motion in the plane of the interferometer is

$$
\bar{v}=V \sin z,
$$

$V$ being the velocity of the absolute motion and $z$ the zenith distance of its apex.
If $\delta \geqq 90^{\circ}-\phi$, it may be seen from the model that the minimum value of $v$ occurs when $z$ is equal to $\delta-\phi$, that its maximum value occurs when $z$ is equal to $180^{\circ}-(\delta+\phi)$ and that the maximum and minimum values occur at times separated by twelve sidereal hours. If the
observations cover the entire sidereal day, the maximum and minimum effects may be obtained. Let $R$ be the ratio of minimum to maximum observed velocities; then

$$
R=v_{\min } / v_{\max }=\sin (\delta-\phi) / \sin (\delta+\phi),
$$

from which the declination of the apex of the absolute motion is derived:

$$
\tan \delta=[(1+R) /(1-R)] \tan \phi
$$

If $\delta<90^{\circ}-\phi$, the line of motion will coincide with the plane of the interferometer twice in each day and the maximum observed velocity, $v_{\max }$, will be equal to the actual velocity $V$. As the minimum velocity occurs when the apex crosses the meridian of the observer, its zenith distance will be $\phi-\delta$ and hence the observed velocity will be the velocity $V$ multiplied by the sine of $\phi-\delta$. Therefore:
and

$$
\begin{aligned}
v_{\min } / v_{\max } & =V \sin (\phi-\delta) / V=\sin (\phi-\delta) \\
\delta & =\phi \pm \sin ^{-1}\left(v_{\min } / v_{\max }\right) .
\end{aligned}
$$

Since the apex dips below the horizon, the observed velocity will have two maximum values during the sidereal day and two minimum values. The maxima occur when the apex crosses the horizon of the observer and the minima when it crosses the meridian. The two maxima coalesce when $\delta=90^{\circ}-\phi$.

## The apex of the absolute motion determined

 from the azimuth of the ether-drift effectFor $\delta \geqq \phi$. From the manner in which the motion of the earth is projected on the plane of the interferometer, Fig. 17, it is evident that the rotation of the earth on its axis from west to east will cause the azimuth of the apex to oscillate back and forth, crossing the meridian twice in each sidereal day at times twelve hours apart. The sidereal time, $\theta_{E-W}$, when the apex crosses the meridian from east to west, is the right ascension of the apex. Then

$$
\alpha=\theta_{E-W} .
$$

If the time, $\theta_{W-E}$, when the apex crosses the meridian from west to east is also determined, then

$$
\alpha=\frac{1}{2}\left(\theta_{E-W}+\theta_{W-E}\right)+6^{h} .
$$

As the azimuth of the effect in the interferometer, which corresponds to the azimuth of the apex, oscillates across the meridian, it reaches a maximum displacement, first to the east and then to the west in each sidereal day. When $\delta \geqq \phi$, this maximum azimuth may be treated as the azimuth of a circumpolar star at its eastern or western elongation. It is shown in treatises on spherical and practical astronomy that the azimuth of elongation depends in a very simple way upon the declination of the star and upon the latitude of the observatory. The relation is:

$$
\sin A_{\max }=\cos \delta / \cos \phi
$$

whence

$$
\cos \delta=\sin A_{\max } \cos \phi
$$

When $\delta \leqq \phi$, the azimuth of the apex swings completely around the horizon in a sidereal day. If $\theta_{E}$ is the sidereal time when the azimuth is due east, then

$$
\tan \delta=\tan \phi \cos \left(\theta_{E}-\alpha\right)
$$

Presuming that the orbital velocity of the earth is known, the formulae now provided are sufficient for the determination in general of the apex and velocity of the absolute motion of the earth, from observations of the relative motion of the earth and ether as made with the interferometer. These observations, giving simply the maximum displacement of the interference fringes as the apparatus turns on its axis, together with the azimuth at which this maximum displacement occurs, must adequately cover the period of one sidereal day for a given epoch. A complete set of such observations gives one determination of the velocity of the absolute motion and two independent determinations of the apex of the motion.

The determination of the direction of the earth's absolute motion is dependent only upon the direction in which the telescope points when the observed displacement of the fringes is a maximum; it is in no way dependent upon the amount of this displacement nor upon the adjustment of the fringes to any particular width or zero position. The actual velocity of the earth's motion is determined by the amplitude of the periodic displacement, which is proportional to the square of the relative velocity of the earth
and the ether and to the length of the light path in the interferometer. The two effects, magnitude and azimuth of observed relative motion, are quite independent of each other.

## Harmonic analysis of the fringe displacements

The records of the actual interferometer observations for the Mount Wilson cycle consist of three hundred and sixteen pages of readings of the positions of the interference fringes, of the form shown in Fig. 8. Each set contains readings for twenty or more turns of the interferometer. The twenty or more readings for each of the sixteen observed azimuths are averaged and the averages are compensated for the slow linear shift of the whole interference system during the period of observation, as explained previously in connection with Fig. 9. The average readings for each set are then plotted on coordinate paper, to a large scale, for the purpose of harmonic analysis. The graphs, I, II, III, and IV, Fig. 21, show the readings for four successive sets of observations made on April 2, 1925. The plotted points are positions of the central black fringe of the interference pattern with respect to the fiducial point, as the interferometer makes one complete turn. The unit for the scale of ordinates is one-hundredth of a fringe width, while the abscissae correspond to azimuth intervals of $22 \frac{1}{2}^{\circ}$, beginning at the north point and proceeding clockwise around the horizon. A chart of this kind is plotted for each set of observations. These charted "curves" of the actual observations contain not only the second-order, halfperiod ether-drift effect, but also a first-order, full-period effect, any possible effects of higher orders, together with all instrumental and accidental errors of observation. The present ether-drift investigation is based entirely upon the second order effect, which is periodic in each half revolution of the interferometer. This secondorder effect is completely represented by the second term of the Fourier harmonic analysis of the given curve. In order to evaluate precisely the ether-drift effect, each curve of observations has been analyzed with the Henrici harmonic analyzer for the first five terms of the Fourier series. The first-order effect in the observation is shown by the fundamental component, which is drawn under the corresponding curve of observa-
tions in Fig. 21; the second-order effect is shown by the curve next below; while the fourth curve in each instance shows the sum of the third, fourth, and fifth components. It is evident that the observed curves contain very little trace of any effects of any higher orders. The residual curves are of very small amplitude and are evidence of the fact that the incidental and random errors are small. The harmonic analysis and synthesis has been performed by methods which have been completely described elsewhere by the writer. ${ }^{12}$
The harmonic analysis of the observations gives directly the amplitude in hundredths of a fringe width and the phase as referred to the north point of the second harmonic of the curve, which is the ether-drift effect. The observed amplitude of the movement of the fringes is at once converted into the equivalent velocity of the relative motion of the earth and ether, as observed in the plane of the interferometer, by means of the relation developed in the elementary theory of the experiment:
and

$$
\begin{aligned}
& d=2 D\left(v^{2} / c^{2}\right) \\
& v=\left(d c^{2} / 2 D\right)^{\frac{1}{2}}
\end{aligned}
$$

$d$ being the observed half-period displacement of the fringes and $D$ the length of the arm of the interferometer, that is the distance from the halfsilvered mirror by means of multiple reflections to the end mirror, No. 8, both being expressed in terms of the effective wave-length of the light used for the interferences; $v$ is the relative motion of the earth and the ether in the plane of the interferometer and $c$ is the velocity of light, both being expressed in kilometers per second. The nomograph, Fig. 20, consists of a parabolic curve which shows the relative velocity corresponding


Fig. 20. Relation of fringe displacement to velocity of etherdrift for $2 D=112,000,000 \lambda$ and $\lambda=5700 \mathrm{~A}$.

[^8]to a fringe displacement as observed in the interferometer used in these experiments. It is for light of wave-length $\lambda=5700 \mathrm{~A}$, and for a total light-path of $2 D=112,000,000 \lambda$. The azimuth of the ether-drift effect is the direction in which the telescope points when the half-period displacement of the fringes is a positive maximum. This azimuth, $A$, is obtained from the phase, $P$, of the second harmonic component of the observations as determined by the analyzer, from the following relation:
$$
A=(1 / 2)\left(P-90^{\circ}\right)
$$

The point thus located is the crest of the curve representing the second component, expressed in degrees, measured from the north point; the $x$-axis of the curves shown in Fig. 21 begins at the


FIG. 21. Harmonic analysis of ether-drift observations.
north point and extends for one turn of $360^{\circ}$, through the east, south and west points of azimuth back to the north point. The figure shows, in the graphs of the second components, what has already been mentioned, that, within $360^{\circ}$ of azimuth for one complete turn, there are two crests of the second component, corresponding to two azimuths $180^{\circ}$ apart, between which the interferometer is incompetent to distinguish. The dispersion of the azimuth readings is much less than $90^{\circ}$ and the necessity for continuity of azimuth indications for successive observations removes the ambiguity as to which zone of
azimuth a reading belongs but it does not, in the end determine whether the direction in the line of motion is plus or minus. The magnitude and direction of the earth's orbital motion are known and since its direction is reversed at epochs six months apart, its combination with a constant cosmical motion gives the resultant motions which are different for the two epochs. The combination of the orbital and cosmical motions will lead to results consistent with the observed effects only when the cosmic motion is taken with the correct sign and thus the ambiguity is removed.

## The Ether-Drift Observations Made at Mount Wilson in 1925-1926

## General program of observation

The ether-drift observations, made by the writer previous to 1925, consist of twenty-five sets of 995 turns made in collaboration with Professor Morley in 1902-1905, eighty-six sets of 1146 turns made in Cleveland in 1922-1924 and one hundred and sixty-six sets of 1181 turns made at Mount Wilson in 1921 and 1924. These experiments had given conclusive evidence of a real effect which was systematic but which was small in magnitude and was inexplicable as to its azimuth. A program was adopted involving an extensive series of observations for the solution of the general problem of ether-drift without any presumed effects. In order to justify general conclusions, it is necessary to have observations extending throughout the twenty-four hours of the day to show the effects of the rotation of the earth on its axis and at several different times of the year to show the effects of the earth's orbital motion. Since the orbital motion is always tangent to the orbit, it will have different directions at different seasons, producing a resultant absolute motion peculiar to each epoch. Such observations were made at Mount Wilson for four epochs, April 1, August 1 and September 15, 1925, and February 8, 1926; the number of sets of observations for these epochs is thirty-six, ninety-six, eighty-three and one hundred and one, respectively, giving a total of 6402 turns. The model shown in Fig. 24 indicates the relative positions of the earth in its orbit for these four epochs. The results obtained from the complete
analysis and reduction of these observations will be given in detail.
It may be noted that these observations have involved the taking of over 200,000 readings of the positions of the interference fringes, requiring that the observer should walk in a small circle, in the dark, while making the readings, a distance of about 160 miles. More than half of these readings were made in the Mount Wilson observations of 1925 and 1926. The latter observations lead to 12,800 single measures of the velocity of the ether-drift and to 25,600 single determinations of the apex of this motion.

## Data of observation

In the manner described there are obtained from each set of observations, corresponding to a given sidereal time: first, the magnitude of the relative motion of the earth and ether as projected on the plane of the interferometer, expressed as a velocity in kilometers per second; ${ }^{\circ}$ and second, the azimuth, measured from the north point, of the line in which this projected motion takes place. These observed quantities for the four epochs are shown graphically in four charts, Fig. 22. Each dot on the upper curve of each chart represents a velocity and directly under it on the lower curve is the corresponding azimuth of a single observation. The solution is based upon the average curve of the observations; as there is considerable dispersion among the single observations, and to eliminate all bias, the average curves have been obtained by simple arbitrary running average for determining twenty equally spaced points on each curve. The observations for April, the first series taken, were not sufficiently numerous at two times of day and ' for these curves only a smaller number of points are available. The average points are shown by the larger dots with circles and the eight heavy line curves, one for magnitudes and one for azimuths for each of the four epochs constitute the material for further consideration.

There are four curves showing the average observed magnitude of the ether-drift effect throughout the sidereal day for the four epochs; each of these curves leads to a determination of the velocity in kilometers per second of the relative motion of the earth and ether and also of the right ascension and declination of the apex

a

c

b


Fig. 22. Single observations and average curves for the ether-drift effect at Mount Wilson in 1925-1926.
of the earth's absolute motion, characteristic of the particular epoch. There are four curves showing the average azimuth of the ether-drift effect throughout a sidereal day, for the four epochs; each of these curves determines the right ascension and declination of the apex of the earth's absolute motion. In all, there are four determinations of the velocity of motion as projected on the plane of the interferometer, one for each epoch, and eight independent determinations of the apex of the motion, two for each epoch.

These observations are to be reduced according to the principles explained in the preceding sections, to determine the positions of the apexes of the resultant motions for the four epochs. From each curve for the magnitude of the effect are to be obtained the numerical values of the maximum and minimum ordinates and the sidereal time of the minimum; from each curve for the azimuth of the effect are to be obtained the maximum oscillation of the azimuth and the two sidereal times when the curve crosses its axis.

The reduction of the observations involves the latitude of the location of the interferometer. The observations here recorded were made at the Mount Wilson Observatory in latitude $+34^{\circ}$ $13^{\prime}$.

It is at once evident from the character of the curves of observation, Fig. 22, that the declination of the apex is greater than the complement of the latitude of the observatory; this is indicated by the fact that the departure of the azimuth curve from its axis is always less than $90^{\circ}$ and by the fact that the magnitude curve shows only a single maximum and a single minimum. This determines the choice of the alternate formulae of calculation. The study of the conditions with the models leads to the same conclusion. Furthermore, the earlier calculations of these observations included the consideration of an apex with a declination smaller than the complement of the latitude, always leading to inconsistent results. Thus the apex is known to be circumpolar in its astronomical relations.

It may be noted that both the direction and the velocity of the ether drift should change from epoch to epoch because the effect is the resultant of the constant cosmic motion of the
earth and of the changing orbital motion and these changes should be systematic and characteristic of the epoch, as will be explained later.

## Final results of observation

Tables I and II give the right ascensions and declinations of the apexes of the observed motion of the earth for the four epochs and for the two alternative directions. In the tables $\alpha-\mathrm{Mag}$ and $\delta$-Mag indicate the values obtained from the magnitude curves, while $\alpha-\mathrm{Az}$ and $\delta$-Az are obtained from the azimuth curves.

Table I. Right ascension of apex.

| Epoch | $\alpha$-Mag |  | $\alpha-\mathrm{Az}$ |  | Mean |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |
| Feb. 8 | $18^{h}$ | $0^{m}$ | $18^{h}$ | $0^{m}$ | $18^{h}$ | $0^{m}$ |  | 0 m |
| Apr. 1 | 15 | 15 |  | 10 | 15 | 42 |  | 42 |
| Aug. 1 |  | 45 | 16 | 10 | 15 | 57 | 3 | 57 |
| Sep. 15 | 17 | 5 | 17 | 0 | 17 | 3 | 5 | 5 |

Table II. Declination of apex.

| Epoch | $\delta$-Mag | $\delta-\mathrm{Az}$ |  | Mean |  |
| :--- | :---: | :--- | :--- | :--- | :---: |
| Feb. 8 | $\pm 79^{\circ} 35^{\prime}$ | $\pm 75^{\circ} 19^{\prime}$ | $\pm 77^{\circ} 22^{\prime \prime}$ |  |  |
| Apr. 1 | $\pm 78$ | 25 | $\pm 75$ | 12 |  |
| Aug. 1 | $\pm 67$ | 30 | $\pm 76$ | 48 |  |
| Sep. 15 | $\pm 61$ | 40 | $\pm 62$ | 4 |  |

Table III. Velocities and displacements.

| Epoch |  | Velocity |
| :---: | :---: | :---: |
| Feb. 8 | $9.3 \mathrm{~km} / \mathrm{sec}$. | $\lambda=5700 \mathrm{~A}$ |
| Apr. 1 | 10.1 | $0.104 \lambda$ |
| Aug. 1 | 11.2 | 0.123 |
| Sep. 15 | 9.6 | 0.152 |
|  |  | 0.110 |

The curves of observation, Fig. 22, give directly the values of the maximum velocity of relative motion of the earth and ether, as observed in the plane of the interferometer, for the four epochs; these velocities are given in Table III. The table also shows the displacements of the interference fringes, in terms of a fringewidth, which would be produced in the interferometer used in these experiments, by the observed velocities of ether drift.

The three tables contain all of the data provided by the three hundred and sixteen sets of observations made at Mount Wilson in 1925 and 1926, for the solution of the ether-drift problem.

In this work the calculations proceed directly from the actual observations, without any presumptions as to the result. All of the original observations have been included in the calculation, without any omissions and without the assignment of weights. No corrections of any kind have been applied to the observed quantities. This procedure has been adopted as the only safe one in the first search for a hitherto unidentified effect. The present results strikingly illustrate the correctness of this method, as it now appears that the forty-six years of delay in finding the effect of the orbital motion of the earth in the ether-drift observations has been due to the efforts to verify certain predictions of the so-called classical theories and to the influence of traditional points of view.

Absolute Motion of the Solar System and The Earth's Orbital Motion Determined
Northern apex of the solar motion rejected
As already explained, the interferometer determines the line in which the motion of the earth with respect to the ether takes place but does not determine the direction of motion in this line. The results of the observations given in Tables I and II indicate either an apex located near the north pole of the ecliptic or one diametrically opposite, near the south pole of the ecliptic. The choice between the two possible directions of motion is determined by the consistency of the results in satisfying the original observations taken as a whole and in connection with known phenomena. The studies of the proper motions and of the motions in the line of sight of stars in our own cluster have shown that the solar system is moving with respect to the nearby stars towards an apex located in the constellation Hercules, about $42^{\circ}$ from the northern one of the two apexes indicated by the interferometer observations, the velocity of this motion being about nineteen kilometers per second. This circumstance seemed confirmatory of an absolute motion towards the north and the northern apex was chosen for further study of the problem.
Upon the completion of the observations for three epochs at Mount Wilson, corresponding to April 1, August 1, and September 15, 1925, a study of the results was made upon the pre-
sumption of a northern apex. Various trial solutions were checked with the parallelogram apparatus, Fig. 18, and finally by a partial least squares solution, for the determination of the velocity of the cosmic motion. The effects which should be characteristic of the several epochs because of the varying direction of the orbital motion could not be identified in the corresponding curves of observation, indicating that the orbital component is probably much smaller than the cosmic component. The curves for the three epochs were simply averaged and it was found that when plotted in relation to local civil time, the curves are in such phase relations that they nearly neutralize each other; the average effect for the three epochs thus plotted is very small and unsystematic. The curves of observation were then plotted with respect to sidereal time and a very striking consistency of their principal characteristics was shown to exist, not only among the three curves for azimuth and those for magnitude, but, what was more impressive, there was a consistency between the two sets of curves, as though they were related to a common cause. The average of the curves, on sidereal time, showed conclusively that the observed effect is dependent upon sidereal time and is independent of diurnal and seasonal changes of temperature and other terrestrial causes and that it is a cosmical phenomenon. The results of this study were presented as the address of the President of the American Physical Society at the meeting in Kansas City, on December 29, 1925. ${ }^{13}$ The conclusion stated that there is a positive, systematic ether-drift effect, corresponding to a constant relative motion of the earth and the ether, which at Mount Wilson has an apparent velocity of ten kilometers per second; and that the variations in the direction and magnitude of indicated motion are exactly such as would be produced by a constant motion of the solar system in space towards an apex, near the north pole of the ecliptic, having a right ascension of $17 \frac{1}{2}$ hours and a declination of $+65^{\circ}$. On the hypothesis of the Stokes ether concept, that the ether is partially entrained by matter moving through it, it was suggested that the observed velocity of ten kilometers per second might be only a fraction of the absolute velocity;
and further, assuming that the earth's orbital velocity of thirty kilometers per second, similarly reduced, would be so small as to be near the limit of perceptibility in these observations, it was suggested that the actual velocity of the cosmical motion might be two hundred kilometers or more, per second. It was also reported that, for some unexpected reason, all the azimuths were displaced to the westward.

A fourth series of observations was made at Mount Wilson, corresponding to the epoch, February 8; 1926, and a reëxamination of all the observations for the four epochs was made, as before, on the presumption of an apex near the north pole of the ecliptic and, because no consistent effect of the orbital motion could be found, the four series of observations were simply averaged for the determination of the cosmical motion of the solar system. The results of this elaborate study were reported at the Pasadena Ether-Drift Conference of February 4 and 5, 1927, ${ }^{14}$ indieating that there is a constant cosmical motion, of the same general characteristics as were reported at Kansas City, the apex having a right ascension of 17 hours and a declination of $+68^{\circ}$. It was understood at this time that the process of averaging the observations for the four epochs eliminated the orbital effect, since two of the positions of the earth in its orbit were nearly diametrically opposite the other two, as is shown in Fig. 24. It was announced at the Pasadena Conference that the orbital effect, if it existed, was certainly small and though the search so far had failed to demonstrate its influence, yet the writer was confident that it would be found and that further study and observation would be carried on for this purpose. It may be added that an adequate analysis and calculation of the observations of the four epochs, upon any one set of assumed conditions, requires the time of an expert computer for perhaps a full year. This and other considerations, such as the making of further observations in Cleveland in 1927 and 1929, have delayed the plan for the restudy of the Mount Wilson observations until the autumn of 1932.

As explained in the next section, the new study of the problem, based upon the presumption of a

[^9] Mt. Wilson Obs. No. 373, 12 (1928).
solar motion directed to the southward, has given consistent results for both the cosmic motion of the solar system and for the orbital motion of the earth. For this reason the northern apex of the solar motion is rejected in favor of the southern apex.

## Southern apex of the solar motion adopted

Beginning in the autumn of 1932, a reanalysis of the ether-drift problem, and a recalculation of the observations made at Mount Wilson in 1925 and 1926 have now been completed. By adopting the alternative possibility that the motion of the solar system is in the cosmic line previously determined but is in the opposite direction, being directed to the apex near the south pole of the ecliptic, a wholly consistent solution has been obtained. This gives for the first time a quantitative determination of the absolute motion of the solar system and a positive detection of the effect of the orbital motion of the earth, by means of the ether-drift interferometer.

The apexes derived from the observations for the four epochs, determined by the right ascensions and declinations given in Tables I and II, are shown on the chart, Fig. 23, which represents the south circumpolar region of the celestial sphere. The observed apexes derived from the azimuth curves are indicated by squares


Fig. 23. Chart of the observed apexes of the resultant absolute motion of the earth.
and those derived from the magnitude curves, by triangles; the means of the two positions for each epoch, indicated by the stars, are the final observed positions of the apexes of the earth's absolute motion for the respective epochs. The four apexes should lie on the earth's "aberration orbit," the center of which is the apex of the cosmic component of the earth's motion. This aberration orbit is the projection of the earth's orbit on the celestial sphere and, since the center is only $7^{\circ}$ from the pole of the ecliptic, the projection, for the purposes of this study, is a circle. The center of the circle which most nearly fits the four observed apexes represented by the stars is found by graphic methods; this center is a first approximation to the apex of the earth's cosmic motion. The four apexes not only lie remarkably close to the circle but they are properly spaced to correspond to their epochs, as indicated by the model of the orbit, Fig. 24.

By means of the triangle law it is now possible to make an approximate solution for the velocity of the earth's cosmic motion. The explanation will be facilitated by means of the model, Fig. 24,


Fig. 24. Model illustrating the positions of the earth in its orbit at the four epochs of observation.
which shows the relative positions of the earth in its orbit for the four epochs; above each of the four globes is a wire parallelogram, approximately to scale, which illustrates the relations of the orbital and cosmic components of motion and their resultant; the cosmical component has a downward direction. The direction and magnitude of the orbital component are known, the direction of the resultant motion is given by the
observations (its magnitude is not required), the direction of the cosmic component is towards the center of the aberration orbit as just found; thus there are given the directions of the three sides of a triangle, and the magnitude of one side, which determines the magnitudes of the other sides. In this manner, a first approximation to the velocity of the cosmic component of motion was found to be 200 kilometers per second.
Having obtained an approximate value for the velocity of the cosmic motion, it is used, by the application of the laws of spherical triangles, to find the apex of the cosmic component; this is done separately for each of the four epochs, by using the directions of the resultant motion given by the four observed resultant apexes and the velocity and directions of the earth's orbital motion appropriate to the four epochs. Thus there are obtained four approximate locations of the apex of the cosmic motion, based upon the assumed velocity; these should coincide with the center of the aberration orbit but probably will be scattered near the center.

Further trials were made, with assumed values for the velocity of the cosmic component of 205, 210 , and 215 kilometers per second, leading to the conclusion that a velocity of 208 kilometers per second, for the cosmic component, gives the closest grouping of the four independently determined locations of the cosmic apex. Table IV gives the right ascensions and declinations of

Table IV. Centers of aberration orbits from observed places.

| Epoch | $\alpha$ |  |
| :--- | :--- | :--- |
| Feb. 8 | $5^{h} 14^{m}$ | $-69^{\circ}$ |
| Apr. 1 | 4 | 46 |
| Aug. 1 | 4 | 40 |
| Sep. 15 | 4 | 54 |
| Mean apex | $4^{h} 54^{m}$ | -70 |
| 4 | 0 |  |

the four points and, also, the mean values of the coordinates, which are adopted as locating the apex of the cosmic motion. The apexes, derived from the observations of each epoch separately, are shown by the four dots near the center of the circle in Fig. 23, while the average value of these positions is indicated by the dot in the circle. This is the final solution for the cosmic compo-
nent of the motion of the earth and is the absolute motion of the solar system as a whole; this cosmic motion of the earth has a velocity of 208 kilometers per second and is directed to the apex having a right ascension of 4 hours and 54 minutes and a declination of $-70^{\circ} 33^{\prime}$.

The location of the apex thus determined is in the constellation Dorado, the Sword-Fish, and is about $20^{\circ}$ south of the star Canopus, the second brightest star in the heavens. It is in the midst of the famous Great Magellanic Cloud of stars. The apex is only about $7^{\circ}$ from the pole of the ecliptic and only $6^{\circ}$ from the pole of the invariable plane of the solar system; thus the indicated motion of the solar system is almost perpendicular to the invariable plane. This suggests that the solar system might be thought of as a dynamic disk which is being pulled through a resisting medium, and which therefore sets itself perpendicular to the line of hotion.

The fact that the sun is moving towards the southern apex with a velocity of 208 kilometers per second and at the same time is apparently moving, with respect to the near-by stars, in the opposite direction towards the constellation Hercules with a velocity of 19 kilometers per second, indicates that the group of stars as a whole is moving towards the southern apex with a velocity of 227 kilometers per second.

## Reduced velocity and displaced azimuth are unexplained

The direction of the earth's motion in space has been determined by assuming that the motion is projected onto the plane of the interferometer and by observing the variations produced in the projected component by the rotation of the earth on its axis and by the revolution around the sun. The velocity of the motion has been obtained by comparison with effects presumed to be produced by the known orbital velocity of the earth. The evaluation of the observed effect is based on the presumption that it is a second order effect and that the ether is wholly stagnant and undisturbed by the motion of the earth through it. There are found to be two facts of observation which are wholly unexplained on this simple theory.
The displacement of the interference fringes has always been less than was expected, indi-
cating a reduced velocity of relative motion, as though the ether through which the interferometer is being carried by the earth's motion were not absolutely at rest. When the values of the velocity of the earth's motion as calculated from the results of this investigation are compared with the velocities observed in the interferometer, there is obtained a quantitative measure of the factor of reduction which has so far remained inexplicable. Table V shows the maximum observed resultant velocities, from Table III, together with the calculated resultant velocities in the plane of the interferometer and the factor of reduction, $k$, for each epoch. The value of $k$ which leads to results most concordant with the actual observations for all epochs is




Fig. 25. Chart showing the observed displacement of the axis of azimuth of the ether-drift.

Table V. Cosmical velocities.

| Epoch |  | Velocity-Obs. | Velocity-Calc. |
| :--- | ---: | :--- | :---: |
| Feb. 8 | $9.3 \mathrm{~km} / \mathrm{sec}$. | $195.2 \mathrm{~km} / \mathrm{sec}$. | $k$ |
| Apr. 1 | 10.1 | 198.2 | 0.048 |
| Aug. 1 | 11.2 | 211.5 | 0.051 |
| Sep. 15 | 9.6 | 207.5 | 0.053 |

## Value adopted for calculations, $k=0.0514$

$k=0.0514$ and this one value has been used in the calculations for the theoretical curves. However, until the physical nature of this reduction factor is understood, it need not be assumed that it should be constant for all epochs. It is assumed that the cosmic component and the orbital component are both reduced in the same proportion.

In accordance with the simple theory, the direction of the cosmic motion should swing back and forth across the north and south line once in each sidereal day, because of the rotation of the earth on its axis. When the observed azimuth of motion is charted, the resulting curve of directions crosses its own axis twice in each day, as shown in Fig. 25, but this axis is variously displaced from the meridian. For the February epoch the axis is displaced $10^{\circ}$ to the west of north; for April the displacement is $40^{\circ}$ east; for August $10^{\circ}$ east, and for September $55^{\circ}$ east.

## Validity of the solution

Every suspected cause of disturbance having been eliminated, and an adequate method of


Fig. 26. The observed and calculated velocity and azimuth of ether-drift for the four epochs of observation, plotted with relation to sidereal time.
procedure having been developed, it is presumed that the persistently observed effects, which though small are systematic, are due to a real ether-drift. The observed displacement of the interference fringes, for some unexplained reason, corresponds to only a fraction of the velocity of the earth in space. The theoretical solution of the problem of absolute motion which has been presented involves only the relative values of the magnitudes of the observed effect and does not require a knowledge of the cause of the reduction in the apparent velocity of the motion nor of the amount of this reduction. The validity of the solution is shown by using the newly found velocity and direction of the cosmic motion together with the known velocity and direction of the orbital motion of the earth for the calculation of the resultant effects for each of the four epochs.

The magnitude and direction of the resultant motion, as projected on the plane of the interferometer, are computed for intervals of two hours throughout the sidereal day for each epoch. The magnitudes multiplied by the reduction factor $k$ are shown in Fig. 26 by the four smooth-line curves at the left. The azimuths of the calculated directions, as referred to the axes of the curves, are shown by the smooth line curves at the right. Superposed on these eight curves are the average curves of the actual observations, taken from Fig. 22.

The calculated curves fit the observations remarkably well, considering the nature of the experiment. Since the cosmical component of motion is relatively large, its effect predominates so that the phases of the curves remain nearly constant when charted on sidereal time; that is, the minima all occur at about 17 hours. It is the orbital component which causes the flattening of the curves for February and April and causes an accentuated minimum six months later. The effect of the orbital component causes the apparent leaning forward in the azimuth curves for August and September.

The closeness with which the critical characteristics of the theoretical curves for the different epochs are followed by the observations is more strikingly shown when the curves are charted with respect to local civil time, as in Fig. 27. The predominating effect of the cosmic com-


Fig. 27. The observed and calculated velocity and azimuth of ether-drift for the four epochs of observation, plotted with relation to civil time.
ponent while remaining constant in sidereal time, causes the minimum which occurs near sunrise in February to move progressively in civil time through the day, as the seasons change, so that in September it occurs near sunset; the time when the azimuth curve crosses its axis likewise shifts progressively in civil time.

Continuing the astronomical description, having found the elements of the aberration orbit of the earth's absolute motion, these are used to compute the apparent places of the observations. The velocity and apex of the constant cosmic component of the earth's motion just found is combined with the known orbital velocity for the dates of the four epochs of observation, to find the four apexes of the resultant motions of the four epochs. The observed and calculated right ascensions and declinations of the apexes are given in Table VI.

Table VI. Resultant apexes, observed and calculated.

| Epoch | $\alpha$-Obs. |  |  |  |  |  |  |  |
| :--- | :---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: |

The apex of the cosmic motion previously determined, given in Table IV, is shown by the
large star in Fig. 28 and the four calculated apexes for the resultant motions at the four epochs are shown by the small circles, which necessarily lie on the circle representing the calculated aberration orbit. The observed apexes for the four epochs are represented by the small stars. The location of the pole of the ecliptic is also shown. The close agreement between the calculated and observed apparent apexes would seem to be conclusive evidence of the validity of the solution of the ether-drift observations for the absolute motion of the earth and also for the effect of the orbital motion of the earth, which hitherto has not been demonstrated.


Fig. 28. Observed and calculated apexes of the absolute motion of the solar system.

It may seem surprising that such close agreement between observed and calculated places can be obtained from observations of such minute effects, and effects which are reputed to be of such difficulty and uncertainty. Perhaps an explanation is the fact that the star representing the final result for the February epoch is, in effect, the average of 8080 single determinations of its location; the star for the August epoch represents 7680 single determinations, that for September, 6640 and that for April, 3208 determinations.
Attention is called to the fact that the results here obtained are not opposed to the results originally announced by Michelson and Morley in 1887; in reality they are consistent with and confirm the earlier results. With additional
observations, the interpretation has been revised and extended.

The model, Fig. 29, represents, to scale, the conclusions of this study of the absolute motion of the earth. The earth is represented by the ball near the top of the model and the plane of the ecliptic is the horizontal plane through the center of the earth. The cosmic component of the earth's motion, which is the absolute motion of


FIG. 29. Model illustrating the components of ether-drift.
the solar system, is directed to the apex near the south pole of the ecliptic and is represented by the arrow near the top of the model and by the rod in its prolongation below the earth. The orbital motions for the four epochs of these observations are represented by the four arrows in the horizontal plane. The four resultant motions are shown by the diagonals of the four parallelograms corresponding to the several epochs. The resultant motion in the course of a year traces on the celestial sphere the aberration orbit of the earth represented by the circle near
the bottom of the model; the four epochal positions are marked by the arrows at the bottom. This part of the model corresponds to the orbital circle on the chart, Fig. 28, and to the model of the orbit with the four globes, Fig. 24.

## Probable error

A study of the numerical results as plotted in Fig. 26 shows that the probable error of the observed velocity, which has a magnitude of from ten to eleven kilometers per second, is $\pm 0.33$ kilometer per second, while the probable error in the determination of the azimuth is $\pm 2.5^{\circ}$. The probable error in the right ascensions and declinations of the polar chart, Fig. 28, is $\pm 0.5^{\circ}$.

## Full-Period Effect

Throughout these experiments, while the attention has been given to the second-order, half-period effect, there has been present a fullperiod, first-order effect of comparable magnitude. The theory of the ether-drift experiment as usually given is exact but it is also abstract, being based upon simplified conditions of the apparatus which never exist in the actual experiment. What actually happens to the interference fringes depends not only upon the ether-drift effect but also upon the geometrical arrangement of the mirrors. The simple theory assumes that the mirrors at the ends of the two arms of the interferometer are perpendicular to the rays of light; this would produce fringes of infinite width, the whole field of view being uniformly illuminated, a critical condition never desired nor used in practice. In order to produce a series of straight fringes, suitable for the measurement of displacements, as shown in Fig. 7, it is necessary that one of the end mirrors be rotated about a vertical axis through a very small angle so that the two virtual interfering planes intersect. The width of the fringes and the number of fringes in the field of view are directly dependent upon this inclination of the end mirror. The angle of incidence of the light on the mirror, as used in these experiments, differs from $0^{\circ}$ by about $\pm 4^{\prime \prime}$. The late Professor W. M. Hicks of University College, Sheffield, has given an elaborate
discussion of the theory, ${ }^{15}$ using methods which are not only rigorous but also general, applying to any adjustment whatever of the optical parts of the apparatus. In the theory of Hicks it is shown that when the periodic variation in the relative phases of the two beams of light in the interferometer takes place with the mirrors adjusted as in actual practice, there is introduced an additional effect which is periodic in a full turn of the instrument. The amplitude of this fullperiod effect, which varies inversely as the width of the fringes being used at the time of observation, is about equal to the amplitude of the etherdrift effect when there are eight fringes in the field of view; with the adjustment usually secured for six fringes in the field of view, the full-period effect is smaller than the half-period effect, as shown in Fig. 21.
The full-period effect, which has usually been overlooked, is present in all of the observations, including the original observations of Michelson and Morley. Hicks called attention to the latter fact and calculated its magnitude. Unfortunately, in none of the observations heretofore made have there been quantitative measurements of the width of the fringes which determines the angle of inclination of the mirror and it is not possible to use the full-period effect for a solution of the problem of ether-drift. However, the approximate number of fringes visible in the field of view has frequently been recorded. A comparison of the width of fringes thus indicated with the magnitude of the full-period effect shows a direct


FIG. 30. The full-period effect; the relation of amplitude to width of fringes.

[^10]linear relation as required by the theory of Hicks; this relation is shown in Fig. 30.

## The Entrained Ether Hypothesis

In order to account for the results here presented, it seems necessary to accept the reality of a modified Lorentz-FitzGerald contraction, or to postulate a viscous or dragged ether. In commenting upon the preliminary report of this work presented to the National Academy of Sciences in April, 1925, Dr. L. Silberstein said: "From the point of view of an ether theory, this set of results, as well as all others previously discovered, is easily explicable by means of the Stokes ether concept, as modified by Planck and Lorentz, and discussed by the writer (Silberstein) in the Philosophical
Magazine." ${ }^{16}$
The theory of Stokes may be described by means of the following sentences selected from Sir Joseph Larmor's treatise on Aether and Matter, pages 10, 13, 35 and 36 :

> As Sir George Stokes was not disposed to admit that the aether could pass freely through the interstices of material bodies in the manner required by Fresnel's views, and as any other theory of its motion which could be consistent with the fact of astronomical aberration required irrotational flow, an explanation of the limitation to that flow had, he considered, to be found. This chain of argument, that motion of bodies disturbs the aether, that aberration requires the disturbance to be differently irrotational, that this can only be explained by the dispersion of incipient rotational disturbance by transverse waves, and further that radiation itself involves transverse undulation, he regards as mutually consistent and self supporting, and therefore, as forming distinct evidence in favor of this view of the constitution of the aether. . . The question then arises how far this explanation will extend to the case in which the aether is entrained by the matter that is moving through it. There are systematic differences in the socalled constant of aberration and in standard star places as determined at different observatories, which might be explained on the hypothesis of a variation in ether drift due to differences in the local coefficient of drag. The drag at any given station may depend more or less upon altitude, local contour and the distribution of large masses of land such as mountain ranges. The ether-drift experiments have never been

[^11]made at sea-level, nor, in fact, at any place except Mount Wilson, with sufficient completeness to give accurate measures of the effects. The evidence now indicates that the drift at Mount Wilson does not differ greatly in magnitude from that at Cleveland and that at sea-level it would probably have about the same value.
The reduction of the indicated velocity of two hundred or more kilometers per second to the observed value of ten kilometers per second may be explained on the theory of the LorentzFitzGerald contraction without assuming a drag of the ether. This contraction may or may not depend upon the physical properties of the solid and it may or may not be exactly proportional to the square of the relative velocities of the earth and the ether. A very slight departure of the contraction from the amount calculated by Lorentz would account for the observed effect. Sir Oliver Lodge in his autobiography says: "I still cling to the idea that the FitzGerald contraction is a reality which must be taken into consideration in any physical contemplation of the universe. ${ }^{117}$

One is compelled, therefore, to consider whether there are possible readjustments of the theories of the ether that will account for the reduction in the observed velocities of absolute motion and for the displaced azimuths. The difficulties presented by these anomalies are certainly not greater than those existing in many other fields of experimental research.

## Other Recent Ether-Drift Experiments

Since the announcement of the evidence of absolute motion of the solar system made at Kansas City in 1925, several other experimenters have performed ether-drift experiments with interferometers of various designs and under various conditions, leading to results which are generally considered to be at variance with the conclusions of this paper. Brief reference to these experiments will be made but without extended analysis.

Dr. Roy J. Kennedy, at Pasadena, used an interferometer with an optical device of original design, giving great sensitivity. ${ }^{18}$ The length of
${ }_{18}^{17}$ O. J. Lodge, Past Years, 206 (1932).
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Astrophys. J. 68, 367 (1928).
the light path, to the end mirror, represented by $D$ in the formula previously given, was 200 centimeters. The apparatus was in a sealed metal case filled with helium. The conclusion was that any indicated ether-drift must be less than 2.5 kilometers per second; this limiting value was later reduced by Illingworth to 1 kilometer per second.

Professor A. Piccard and E. Stahel, of Brussels, thinking that the height above the earth's surface might influence the ether-drift effect, placed an interferometer in a balloon which ascended to an altitude of 2500 meters. ${ }^{19}$ The balloon was rotated about a vertical axis by means of a propeller. The interferometer had a light path in which $D$ was 280 centimeters; it had a self-recording device and a thermostatic control; it was enclosed in a metal case which was evacuated. The indicated velocity of ether-drift might have been as large as 7 kilometers per second, which was the limit of precision. This interferometer was later taken to the summit of the Rigi in Switzerland, at an altitude of 1800 meters, where the observations showed an upper limit to the possible ether-drift of 1.5 kilometers per second. ${ }^{20}$

The late Professor Michelson, together with F. G. Pease and F. Pearson, used an interferometer mounted in the laboratory of the Mount Wilson Observatory in Pasadena, having a light path, $D$, equal to 1616 centimeters, which was later increased to 2592 centimeters. The readings were made in the vertical axis of the interferometer, the observer being located in the room above the apparatus. "The results gave no displacement as great as one-fiftieth of that to be expected on the supposition of an effect due to a motion of the solar system of three hundred kilometers per second. ${ }^{\prime 21}$

Professor Georg Joos, working at Jena, used an interferometer mounted on a quartz base suspended in an evacuated metal housing and provided with photographic registration. The interferometer had a light path, $D$, equal to 2099

[^12]centimeters. The results indicated that any existing ether drift could not exceed 1 kilometer per second. ${ }^{22}$

In three of the four experiments, the interferometers have been enclosed in heavy, sealed metal housings and also have been located in basement rooms in the interior of heavy buildings and below the level of the ground; in the experiment of Piccard and Stahel, a metal vacuum chamber alone was used and in the experiment of Michelson, Pease and Pearson, the interferometer was in the constant temperature vault but did not have a vacuum case. If the question of an entrained ether is involved in the investigation, it would seem that such massive and opaque shielding is not justifiable. The experiment is designed to detect a very minute effect on the velocity of light, to be impressed upon the light through the ether itself, and it would seem to be essential that there should be the least possible obstruction between the free ether and the light path in the interferometer. It is planned to make a direct study of this factor of the problem.

In none of these other experiments have the observations been of such extent and of such continuity as to determine the exact nature of the diurnal and seasonal variations.

While the interferometer used by Kennedy is more sensitive than that of ordinary type, it is doubtful whether the precision of the result equals that obtained from the very large number of readings made under all conditions of temperature and season with the interferometer of the usual type which is much less sensitive to disturbing causes.

The limitations of the direct-reading method have been recognized but it has been adopted because of its simplicity and because it permits the accumulation of a large number of readingsin the shortest time. It is believed that any lack of precision in making a single reading is fully compensated by the large number of readings and by the use of an interferometer of longer light. path and therefore of greater initial sensitivity. The interferometer used in the experiments here reported has a light-path, $D$, equal to 3203 centimeters.

[^13]
## Other Evidences of Cosmic Motion

The various astronomical determinations of motion of the solar system in space, by the nature of the methods employed, indicate relative motion and do not directly give any information as to an absolute motion. However, several recent important experiments in diverse fields seem to give evidence of a cosmic motion. Dr. Esclangon, Director of the Paris Observatory, has made elaborate studies of earth tides (deformation of the earth's crust) and of ocean tides. In the latter work he considered 166,500 observations extending over a period of nineteen years. ${ }^{23}$ There are component tidal effects which indicate a motion of the solar system in the plane which contains the sidereal time meridian of $4 \frac{1}{2}{ }^{h}$ and $16 \frac{1}{2}{ }^{h} .{ }^{23}$
By a study of the reflection of light, Esclangon finds strong evidence for what he calls an "optical dissymmetry of space" with its axis of symmetry in the meridian of 8 hours and 20 hours, sidereal time. This effect would be explained by an ether-drift and the results are in striking agreement with the ether-drift observations here reported. ${ }^{24}$

Many recent observations on cosmic rays show a very definite maximum of radiation in the direction indicated by the meridian of 5 hours and 17 hours, sidereal time. The very extensive observations of Kolhörster and von Salis, Büttner and Feld and of Steinke all show this effect. ${ }^{25}$ Observations made on the nonmagnetic ship "Carnegie" show the same effect for the observations made between $30^{\circ}$ north and $30^{\circ}$ south latitude. ${ }^{26}$
Evidences of galactic motions which are related more or less directly to the absolute motion of the solar system have been found by Harlow Shapley studying interstellar matter, by J. S. Plaskett from investigation of the motion of $B$-type stars, and by G. Strömberg from researches on star clusters and nebulae. ${ }^{27}$

[^14]L. Courvoisier has made researches of several types to discover evidences of the absolute motion of the earth. His experiments relate to the reflection of light, the deformation of the earth, the elongations of Jupiter's satellites, and to the aberration constant. R. Tomaschek and W. Schaffernicht have made observations on related subjects. ${ }^{28}$

There are several anomalies in astronomical observations of less definite character, which, however, might be explained by the existence of an ether drift. Such anomalies occur in connection with the observed constant of aberration, standard star places and clock corrections determined at different times of day.

Karl G. Jansky of the Bell Telephone Laboratories has found evidences of a peculiar hissing sound in short wave radio reception, which comes from a definite cosmic direction lying in the meridian of 18 hours sidereal time. ${ }^{29}$

## Acknowledgments

The experiments here presented have involved the taking of an enormous amount of observational material, by far the greater part of which was for the purpose of making adjustments and for preliminary trials of conditions; while only the smaller portion, which is still very large, has been used in the final calculations. The reduction of this mass of material has been exceedingly laborious. No other experiment comes to mind which has involved such an amount of detail and such extended study. This has required considerable attention from many different persons. The writer is under special obligation to Professor J. J. Nassau, of the Department of Astronomy of Case School of Applied Science, for very great assistance in the analysis and in the mathematical solution of the numerical and astronomical features of the work since the beginning of the Mount Wilson observations in 1921. Dr. G. Strömberg and other members of the staff of the Mount Wilson Observatory have given advice and assistance of

[^15]the greatest value. Several research assistants have each, for considerable periods, been identified with the experimental work and the reduction and calculation of the observations; among these the following should be especially mentioned: R. F. Hovey (1920-1923), H. A. Pritchard (1923), Willard Samuelson (1924), G. Brooks Earnest (1925), F. W. Taylor (19251926), Donald H. Spicer (1926-1927) and James R. McKinney (1932-1933). Dr. R. M. Langer was a most efficient assistant throughout all the observations made at Mount Wilson in 1925 and 1926, which constitute the principal material for the conclusions of the present report. Professor Phillip M. Morse assisted very effectively in the first analysis of the general problem of the absolute motion of the solar system, and he made a considerable part of the calculations for the
first solution of this problem in 1925-1926. The writer's research associates, Professor John R. Martin (1927-1931) and Mr. Robert S. Shankland (1932-1933), have been directly associated with the restudy of the problem which has resulted in the final determination of the absolute motion of the solar system and the orbital motion of the earth as presented in this report.
Case School of Applied Science has made possible the continuous prosecution of the study of the ether-drift problem. The Carnegie Institution of Washington and the Mount Wilson Observatory made available the exceptional facilities of Mount Wilson for observational work from 1921 to 1926. Mr. Eckstein Case provided funds for the very considerable expenses involved in making the elaborate series of experiments and tests.


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